

Contents

5	Big bang nucleosynthesis	79
5.1	Equilibrium	79
5.2	Neutron-proton ratio	81
5.3	Bottlenecks	82
5.4	Calculation of the helium abundance	83
5.5	Why so late?	85
5.6	The most important reactions	85
5.7	BBN as a function of time	87
5.8	Primordial abundances as a function of the baryon/photon ratio	89
5.9	Comparison with observations	89

5 Big bang nucleosynthesis

One quarter (by mass) of baryonic matter in the universe is helium, heavier elements make up a few percent, and the rest is hydrogen. The building blocks of atomic nuclei, nucleons (i.e. protons and neutrons) are formed in the QCD crossover at $T \sim 150$ MeV and $t \sim 30 \mu\text{s}$. Elements heavier than lithium, up to iron, cobalt, and nickel have been made from lighter elements in fusion reactions in stars. Heavier elements have been formed in supernova explosions and in stellar collisions. However, the amount of helium and some other light isotopes in the universe cannot be understood by stellar mechanisms. It turns out that ^2H , ^3He , ^4He , and ^7Li were mainly produced already during the first hour of the universe, in a process called big bang nucleosynthesis (BBN).

Nucleons and antinucleons annihilated each other soon after the QCD crossover, and the small excess of nucleons left over from annihilation did not have a significant effect on the expansion and thermodynamics of the universe when the universe became matter-dominated at $t_{\text{eq}} \approx 1000 \omega_m^{-2}$ years $\approx 50\,000$ years. The ordinary matter in the present universe is built from this small excess of nucleons. Let us now consider what happened to it in the early universe. We will focus on the period when the temperature fell from $T \sim 10$ MeV to $T \sim 10$ keV (from $t \sim 0.01$ s to a few hours).

5.1 Equilibrium

After the electroweak crossover, the total number of nucleons minus antinucleons is constant due to baryon number conservation. In the temperature range under consideration, the number density of antinucleons is negligible. The baryon number can be in the form of protons and neutrons or nuclei. The weak interaction converts neutrons and protons into each other and the strong interaction builds nuclei from them.

During the period of interest the nucleons and nuclei are nonrelativistic ($T \ll m_p$). Assuming thermal equilibrium, the number density of nucleus of type i is

$$n_i = g_i \left(\frac{m_i T}{2\pi} \right)^{3/2} e^{\frac{\mu_i - m_i}{T}}. \quad (5.1)$$

The proton and neutron masses are

$$m_p = 938.272 \text{ MeV} , \quad m_n = 939.565 \text{ MeV} . \quad (5.2)$$

If the nuclear reactions needed to build nucleus i (with mass number A_i and charge Z_i) from the nucleons,

$$(A_i - Z_i)n + Z_i p \leftrightarrow i + \gamma ,$$

occur at sufficiently high rate to maintain chemical equilibrium, we have

$$\mu_i = (A_i - Z_i)\mu_n + Z_i\mu_p \quad (5.3)$$

for the chemical potentials. For free nucleons we have

$$\begin{aligned} n_p &= 2 \left(\frac{m_p T}{2\pi} \right)^{3/2} e^{\frac{\mu_p - m_p}{T}} \\ n_n &= 2 \left(\frac{m_n T}{2\pi} \right)^{3/2} e^{\frac{\mu_n - m_n}{T}} , \end{aligned} \quad (5.4)$$

$\frac{A_i}{Z_i}$	B_i	g_i
${}^2\text{H}$	2.22 MeV	3
${}^3\text{H}$	8.48 MeV	2
${}^3\text{He}$	7.72 MeV	2
${}^4\text{He}$	28.3 MeV	1
${}^{12}\text{C}$	92.2 MeV	1

Table 1. Some of the lightest nuclei and their binding energies.

so we can express n_i in terms of the neutron and proton densities,

$$n_i = g_i A_i^{\frac{3}{2}} 2^{-A_i} \left(\frac{2\pi}{m_N T} \right)^{\frac{3}{2}(A_i-1)} n_p^{Z_i} n_n^{A_i-Z_i} e^{B_i/T} , \quad (5.5)$$

where

$$B_i \equiv Z_i m_p + (A_i - Z_i) m_n - m_i \quad (5.6)$$

is the binding energy of the nucleus. Here we have approximated $m_p \approx m_n \approx m_i/A$ outside the exponent, and denoted this quantity, the *nucleon mass*, by m_N .

The number densities add up to the total baryon number density

$$\sum A_i n_i = n_b . \quad (5.7)$$

We can express the baryon number density n_b in terms of two observational quantities: the photon density

$$n_\gamma = \frac{2}{\pi^2} \zeta(3) T^3 \quad (5.8)$$

and the *baryon/photon ratio*

$$\frac{n_b}{n_\gamma} = \frac{g_{*s}(T)}{g_{*s}(T_0)} \eta \quad (5.9)$$

to get

$$n_b = \frac{g_{*s}(T)}{g_{*s}(T_0)} \eta \frac{2}{\pi^2} \zeta(3) T^3 . \quad (5.10)$$

After electron-positron annihilation we have $g_{*s}(T) = g_{*s}(T_0)$ and $n_b = \eta n_\gamma$. The quantity η is the baryon/photon ratio today, it is not a function of time. Its value is, from a combination of Planck CMB data and BBN data, $\eta = (6.104 \pm 0.058) \times 10^{-10}$ [1].

For temperatures $m_N \gg T \gtrsim B_i$ we have

$$(m_N T)^{3/2} \gg T^3 \gg n_b > n_p, n_n ,$$

so (5.5) implies that

$$n_i \ll n_p, n_n$$

for $A_i > 1$. So initially there are only free neutrons and protons in large numbers.

5.2 Neutron-proton ratio

What can we say about n_p and n_n ? Protons and neutrons are converted into each other by the weak interaction in the reactions

$$\begin{aligned} n + \nu_e &\leftrightarrow p + e^- \\ n + e^+ &\leftrightarrow p + \bar{\nu}_e \\ n &\leftrightarrow p + e^- + \bar{\nu}_e . \end{aligned} \quad (5.11)$$

If these reactions are in equilibrium, we have $\mu_n + \mu_{\nu_e} = \mu_p + \mu_e$, and the neutron/proton ratio is

$$\frac{n_n}{n_p} = e^{-Q/T + (\mu_e - \mu_{\nu_e})/T} , \quad (5.12)$$

where $Q \equiv m_n - m_p = 1.293$ MeV.

We need to know the chemical potentials of electrons and electron neutrinos. The universe is electrically neutral, so the number density of electrons (or $n_{e^-} - n_{e^+}$) equals the number density of protons, and μ_e can be calculated in terms of η and T . In the ultrarelativistic limit ($T \gg m_e$)

$$n_{e^-} - n_{e^+} = \frac{2T^3}{6\pi^2} \left[\pi^2 \frac{\mu_e}{T} + \left(\frac{\mu_e}{T} \right)^3 \right] = n_p^* < n_b \approx \eta n_\gamma = \eta \frac{2}{\pi^2} \zeta(3) T^3 . \quad (5.13)$$

Recall that n_p^* includes all protons, including those inside nuclei. Since η is small, we have $\mu_e \ll T$, and we can drop the $(\mu_e/T)^3$ term, so

$$\frac{\mu_e}{T} \lesssim \frac{6}{\pi^2} \zeta(3) \eta \approx 4 \times 10^{-10} \ll 1 . \quad (5.14)$$

The nonrelativistic limit can be dealt with in a similar manner. It turns out that μ_e rises as T falls, and somewhere between $T = 30$ keV and $T = 10$ keV it becomes larger than T , and, in fact, comparable to m_e .

For $T \gtrsim 30$ keV, we have $\mu_e \ll T$, and we can drop μ_e in (5.12).

We have not measured the cosmic neutrino background, so we don't know the neutrino chemical potentials.¹ Usually it is assumed that the neutrino asymmetry is

¹Because low-energy neutrinos interact so weakly, it is quite difficult to measure them. The proposed PTOLEMY experiment would measure the neutrino background, see <https://ptolemy.lngs.infn.it/>.

small, like the baryon asymmetry, so $|\mu_{\nu_e}| \ll T$. Neutrino oscillations tend to equilibrate the different neutrino chemical potentials. Since the mu and tau neutrinos do not directly participate in BBN, the main effect of their chemical potential is to increase the effective number of neutrino species. There is currently some disagreement between measurements of the ^4He abundance. If we assume that all neutrino chemical potentials are the same, a conservative observational upper limit from BBN that holds regardless of which of the measurements is correct is $|\mu_{\nu_i}|/T \lesssim 0.1$ [2]. If we keep the muon and tau neutrino chemical potentials separate, the limit for μ_{ν_e} stays about the same, while $|\mu_{\nu_i}|/T \lesssim 1$ for $i = \mu, \tau$. Ignoring both μ_e and μ_{ν_e} , we get the equilibrium neutron/proton ratio

$$\frac{n_n}{n_p} = e^{-Q/T} . \quad (5.15)$$

This equation is not valid for $T \lesssim 30$ keV, since then μ_e is no longer small, but we will use it only at higher temperature.

We can thus express the number densities of all nuclei in terms of the free proton number density n_p , as long as chemical equilibrium holds.

5.3 Bottlenecks

We define the *mass fraction* of nucleus i (here protons and neutrons are counted as nuclei)

$$X_i \equiv \frac{A_i n_i}{n_b} . \quad (5.16)$$

Since

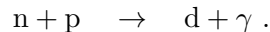
$$n_b = \sum_i A_i n_i , \quad (5.17)$$

we have $\sum X_i = 1$.

Using also the normalisation condition (5.17), we get all equilibrium abundances as a function of T (they also depend on the value of the parameter η).² There are two items to note:

1. The normalisation condition (5.17) includes all nuclei, resulting in a huge polynomial equation from which to solve X_p .
2. In practice we don't have to care about item 1, since as the temperature falls the nuclei no longer follow their equilibrium abundances. The reactions are in equilibrium only at high temperatures, when the other equilibrium abundances except X_p and X_n are small, and we can use the approximation $X_n + X_p = 1$.

In the early universe the baryon density is too low and the time available is too short for reactions involving three or more incoming nuclei to occur at any appreciable rate. Nuclei are built sequentially in lighter nuclei in two-particle reactions, so deuterium is formed first in the reaction



²For n_p and n_n we know just their ratio, since we do not know μ_p and μ_n , only that $\mu_p = \mu_n$. Therefore this extra equation is needed to solve for all n_i .

Only when deuterium nuclei are available can helium nuclei be formed, and so on. This process has bottlenecks: the lack of sufficient densities of lighter nuclei hinders the production of heavier nuclei, and prevents them from following their equilibrium abundances.

As the temperature falls, the equilibrium abundances rise fast. They become large later for nuclei with smaller binding energies. Since deuterium is formed directly from neutrons and protons it can follow its equilibrium abundance as long as there are large numbers of free neutrons available. Since the deuterium binding energy is rather small, the deuterium abundance becomes large rather late (at $T < 100$ keV). Therefore heavier nuclei with larger binding energies, whose equilibrium abundances would become large earlier, cannot be formed. This is the *deuterium bottleneck*³. Only when there is enough deuterium ($X_d \sim 10^{-3}$) can helium be produced in large numbers.

Because the nuclei are positively charged, they repel each other electromagnetically. The nuclei need large kinetic energies to overcome this Coulomb barrier and get within the range of the strong interaction. Thus the cross sections for these fusion reactions fall rapidly with energy and nuclear reactions freeze out when the temperature falls below $T \sim 30$ keV. For this reason there is less than one hour available for nucleosynthesis. Because of the short duration and additional bottlenecks (e.g. there are no stable nuclei with $A = 8$), only very small amounts of elements heavier than helium are formed.

5.4 Calculation of the helium abundance

Let us now calculate the numbers. For $T > 0.1$ MeV, we still have $X_n + X_p \approx 1$, so the equilibrium abundances are

$$X_n = \frac{e^{-Q/T}}{1 + e^{-Q/T}} \quad \text{and} \quad X_p = \frac{1}{1 + e^{-Q/T}} . \quad (5.18)$$

Nucleons follow these equilibrium abundances until neutrinos decouple at $T_D \sim 0.8$ MeV, shutting off the weak $n \leftrightarrow p$ reactions. After this, free neutrons decay, so

$$X_n(t) = X_n(t_{\text{dec}}) e^{-(t-t_{\text{dec}})/\tau_n} , \quad (5.19)$$

where $\tau_n = 878.3 \pm 0.4$ s is the mean lifetime of a free neutron [1]. (The half-life is $\tau_{1/2} = (\ln 2)\tau_n$.) In reality, the decoupling and thus the shift from behaviour (5.18) to behaviour (5.19) is smooth, but an approximation where it is taken to be instantaneous at time t_{dec} when $T_{\text{dec}} = 0.8$ MeV, so $X_n(t_{\text{dec}}) = 0.1657$, gives a fairly accurate final result.

From (5.5) we get the equilibrium mass fractions

$$X_i = \frac{1}{2} X_p^{Z_i} X_n^{A_i - Z_i} g_i A_i^{\frac{5}{2}} \epsilon^{A_i - 1} e^{B_i/T} \quad (5.20)$$

where

$$\epsilon \equiv \frac{1}{2} \left(\frac{2\pi}{m_N T} \right)^{3/2} n_b = \frac{1}{\pi^2} \zeta(3) \left(\frac{2\pi T}{m_N} \right)^{3/2} \frac{g_{*s}(T)}{g_{*s}(T_0)} \eta \sim \left(\frac{T}{m_N} \right)^{3/2} \eta .$$

³Some people prefer to make clear distinction between the nucleus and the atom, calling the former deuteron and the latter deuterium, and similarly for other isotopes.

The factors which change rapidly with T are $\epsilon^{A_i-1}e^{B_i/T}$. For temperatures $m_N \gg T \gg B_i$ we have $e^{B_i/T} \sim 1$ and $\epsilon \ll 1$. Thus $X_i \ll 1$ for others ($A_i > 1$) than protons and neutrons. As temperature falls, ϵ becomes even smaller and at $T \sim B_i$ we have $X_i \ll 1$ still. The temperature has to fall below B_i by a large factor before the factor $e^{B_i/T}$ wins and the equilibrium abundance becomes large.

Deuterium has $B_d = 2.22$ MeV, and $\eta = 6 \times 10^{-10}$, so we get $\epsilon e^{B_d/T} = 1$ at $T_d = 0.06$ MeV: the deuterium abundance becomes large close to this temperature. Since ${}^4\text{He}$ has a much higher binding energy, $B_4 = 28.3$ MeV, the corresponding situation $\epsilon^3 e^{B_4/T} = 1$ occurs at the higher temperature $T_4 = 0.3$ MeV. But as we noted earlier, only deuterium stays close to its equilibrium abundance once it gets large. Helium begins to form only when there is sufficient deuterium available, in practice slightly above T_d . Helium then forms rapidly. The available number of neutrons sets an upper limit to ${}^4\text{He}$ production. Since helium has the highest binding energy per nucleon (of all isotopes below $A = 12$), almost all neutrons end up in ${}^4\text{He}$, and only small amounts of the other light isotopes, ${}^2\text{H}$, ${}^3\text{H}$, ${}^3\text{He}$, ${}^7\text{Li}$, and ${}^7\text{Be}$, are produced.

The Coulomb barrier shuts off the nuclear reactions before heavier nuclei ($A > 8$) have time to form. We get a fairly good approximation for ${}^4\text{He}$ production by assuming instantaneous nucleosynthesis at $T = T_{\text{ns}} \approx 1.1T_d \approx 70$ keV, with all neutrons ending up in ${}^4\text{He}$, so

$$X_4 \approx 2X_n(T_{\text{ns}}) . \quad (5.21)$$

The coefficient 2 comes from the fact that each ${}^4\text{He}$ nucleus has 2 neutrons and mass number $A = 4$, and $4/2 = 2$. After electron-positron annihilation ($T \ll m_e = 0.511$ MeV) the time-temperature relation is

$$t \approx \frac{2.42}{\sqrt{g_*}} \left(\frac{T}{\text{MeV}} \right)^{-2} \text{ s} , \quad (5.22)$$

where $g_* = 3.363$. Since most of the time in the temperature range $T = 0.07$ MeV...0.8 MeV is spent at the lower part, this formula gives a good approximation for the time,

$$t_{\text{ns}} - t_{\text{dec}} = 267 \text{ s} \quad (\text{in reality } 264.3 \text{ s}).$$

Thus we get for the final ${}^4\text{He}$ abundance

$$X_4 = 2X_n(t_{\text{dec}})e^{-(t_{\text{ns}}-t_{\text{dec}})/\tau_n} = 24.5 \text{ \%}. \quad (5.23)$$

The result of numerical calculations for X_4 as a function of η is shown in figure 4 (there called Y).

This calculation of the helium abundance X_4 involves a bit of cheating in the sense that we have used results of accurate numerical calculations to infer that we need to use $T = 0.8$ MeV as the neutrino decoupling temperature, and $T_{\text{ns}} = 1.1T_d$ as the “instantaneous nucleosynthesis” temperature, to best approximate the correct behaviour. However, it gives us a rough quantitative description of what is going on and an understanding of how the helium yield depends on the different factors.

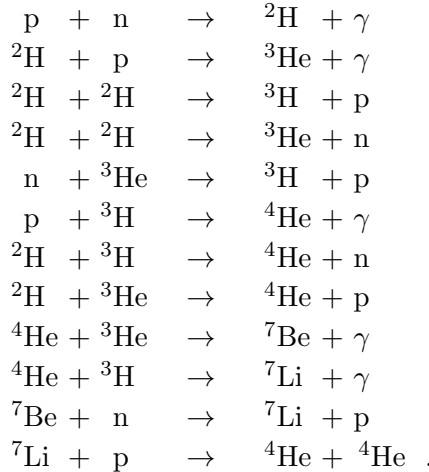
Exercise. Find the dependence of X_4 on η , i.e. calculate $dX_4/d\eta$.

5.5 Why so late?

Let us return to the question of why the temperature has to fall so much below the binding energy before the equilibrium abundances become large. From the energetics we might conclude that when typical kinetic energies, $\langle E_k \rangle \approx \frac{3}{2}T$, are smaller than the binding energy, it would be easy to form nuclei but difficult to break them. Above we saw that the smallness of the factor $\epsilon \sim (T/m_N)^{3/2}\eta$ is the reason why this is not so. Here $\eta = 6 \times 10^{-10}$ and $(T/m_N)^{3/2} \sim 10^{-6}$ (for $T \sim 0.1$ MeV). The main culprit is the small baryon/photon ratio. Since there are $\sim 10^9$ photons for each baryon, there is a sufficient amount of photons who can disintegrate a nucleus in the high-energy tail of the photon distribution, even at rather low temperatures. This is similar to how atoms form at $T \sim 0.3$ eV, even though the hydrogen ionisation energy is 13.6 eV.

5.6 The most important reactions

In reality, neither neutrino decoupling nor nucleosynthesis are instantaneous processes. Accurate results require a rather large numerical computation where one uses the cross sections of all the relevant weak and strong interactions. These cross sections are energy-dependent. Integrating them over the energy and velocity distributions and multiplying with the relevant number densities leads to temperature-dependent reaction rates. The most important reactions are the weak $n \leftrightarrow p$ reactions (5.11) and the following strong reactions (see figure 1)⁴:



In principle, all of these nuclear cross sections are determined by just a few parameters in QCD. However, calculating these cross sections from first principles is too difficult in practice. Instead cross sections measured in the laboratory are used. In contrast, cross sections of the weak reactions (5.11) are known from theory. The relevant reaction rates are now known sufficiently accurately so that the nuclear abundances produced in BBN (for a given value of η) can be calculated with better accuracy than the present abundances can be measured from astronomical observations.

⁴The reaction chain that produces helium from hydrogen in BBN is not the same that occurs in stars. The conditions in stars are different: there are no free neutrons and the temperatures are lower, but the densities are higher and there is more time available. In addition, second and later generations of stars contain heavier nuclei (C, N, O) that act as catalysts in helium production.

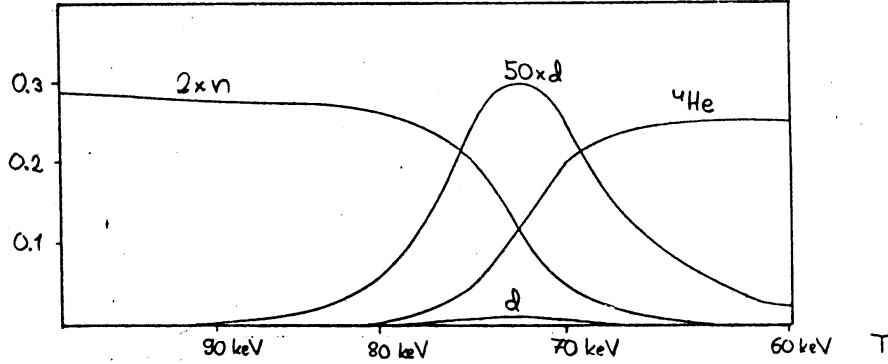


Figure 2: The time evolution of the n , ${}^2\text{H}$ (written as d) and ${}^4\text{He}$ abundances during BBN. Notice how the final ${}^4\text{He}$ abundance is determined by the n abundance before nuclear reactions begin. Only a small part of the neutrons decay or end up in other nuclei. Before becoming ${}^4\text{He}$, all neutrons pass through ${}^2\text{H}$. To improve the visibility of the deuterium curve, we have plotted it also as multiplied by a factor of 50. The other abundances (except p) remain so low, that to see them the figure should be redrawn in logarithmic scale. This plot is for $\eta = 6 \times 10^{-10}$. The time at $T = (90, 80, 70, 60)$ keV is (152, 199, 266, 367) s. Thus the action peaks at about $t = 4$ min.

${}^1\text{H}=p$ we had already before BBN). Their production in the BBN can be calculated, and there is only one free parameter, the baryon/photon ratio. It is directly related to the baryon density as follows:

$$\eta \equiv \frac{n_{b0}}{n_{\gamma 0}} = \frac{\rho_{b0}}{\rho_{\gamma 0}} \frac{\rho_{\gamma 0}}{m_N n_{\gamma 0}} = \frac{\omega_b}{\omega_\gamma} \frac{\pi^4 T_0}{30 \zeta(3) m_N} = 2.74 \times 10^{-8} \omega_b ,$$

where ρ_{b0} is the density of baryonic matter today, and $\omega_b = \Omega_{b0} h^2$ as before.

5.7 BBN as a function of time

Nucleosynthesis as a function of time (or temperature) is shown in figure 2, and in more detail on a logarithmic scale in figure 3. The nuclei ${}^2\text{H}$ and ${}^3\text{H}$ are intermediate states through which reactions proceed towards ${}^4\text{He}$. Therefore their abundance first rises, is highest at the time when ${}^4\text{He}$ production is fastest, and then falls as baryonic matter ends up in ${}^4\text{He}$. The isotope ${}^3\text{He}$ is also an intermediate state, but the main channel from ${}^3\text{He}$ to ${}^4\text{He}$ is via ${}^3\text{He}+n \rightarrow {}^3\text{H}+p$, which is extinguished early as the free neutrons are used up. Therefore the abundance of ${}^3\text{He}$ does not fall the same way as those of ${}^2\text{H}$ and ${}^3\text{H}$. The abundance of ${}^7\text{Li}$ also rises at first and then falls via ${}^7\text{Li}+p \rightarrow {}^4\text{He}+{}^4\text{He}$. Since ${}^4\text{He}$ has a higher binding energy per nucleon, B/A , than ${}^7\text{Li}$ and ${}^7\text{Be}$ have, these also want to return into ${}^4\text{He}$. This does not happen to ${}^7\text{Be}$, however, since, just like for ${}^3\text{He}$, the free neutrons needed for the reaction ${}^7\text{Be}+n \rightarrow {}^4\text{He}+{}^4\text{He}$ have almost disappeared.

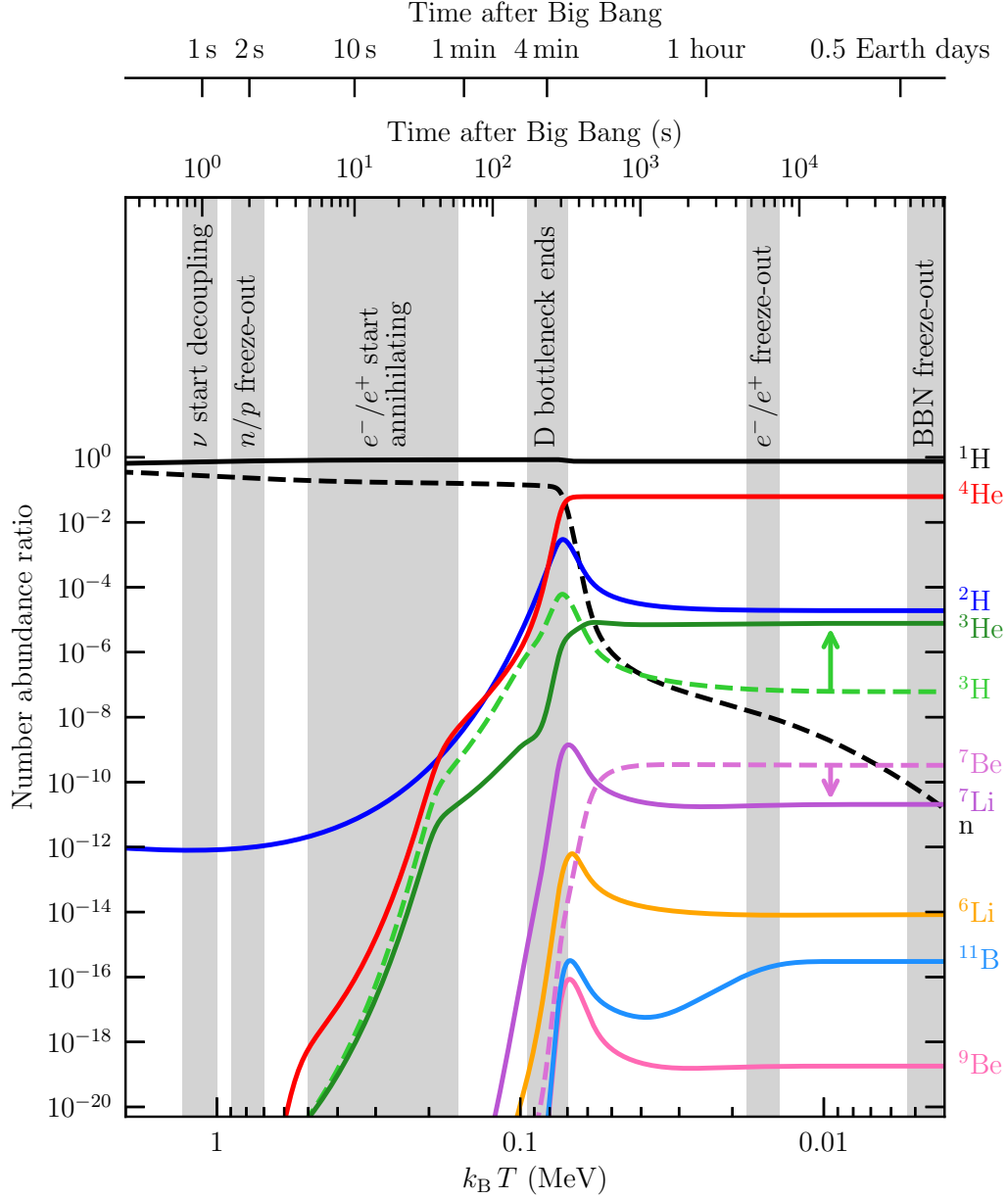


Figure 3: The time evolution of the abundance of n and various nuclei on a logarithmic scale during BBN, with various cosmological milestones marked with gray bands [3]. Note that the $e^+ - e^-$ annihilation in reality lasts throughout BBN, and only ends at around 2 hours, after nuclear fusion reactions have shut down.

	B(MeV)	B/A
^2H	2.2245	1.11
^3H	8.4820	2.83
^3He	7.7186	2.57
^4He	28.2970	7.07
^6Li	31.9965	5.33
^7Li	39.2460	5.61
^7Be	37.6026	5.37
^{12}C	92.1631	7.68
^{56}Fe	492.2623	8.79

5.8 Primordial abundances as a function of the baryon/photon ratio

Let us consider BBN as a function of η , shown in figure 4. The larger η , the higher the number density of nucleons. The reaction rates are faster and nucleosynthesis can proceed further. This means that a smaller fraction of intermediate nuclei, ^2H , ^3H , and ^7Li are left over – the burning of nuclear matter into ^4He is cleaner. Also ^3He production falls with increasing η . However, ^7Be production increases with η . In the figure we have plotted the final BBN yields, so ^3He is the sum of ^3He and ^3H , and ^7Li is the sum of ^7Li and ^7Be . The complicated shape of the $^7\text{Li}(\eta)$ curve is due to these two contributions: 1) For small η we get lots of directly produced ^7Li , whereas 2) for large η there is very little directly produced ^7Li , but a lot of ^7Be is produced. In the middle, at $\eta = 3 \times 10^{-10}$, there is a minimum of ^7Li production where neither channel is very effective.

The ^4He production increases with η , since if the density is higher, then nucleosynthesis begins earlier, when there are more neutrons left.

5.9 Comparison with observations

Abundances of the various isotopes calculated from BBN can be compared to the observed abundances. The comparison of theory and observations complicated by *chemical evolution*, i.e. nuclear reactions in stars. BBN gives the primordial abundances of the isotopes. The first stars form with this element composition. In stars, further fusion reactions take place and the composition of the star changes with time. Towards the end of its life, the star ejects its outer parts into interstellar space, and the processed material mixes with primordial material. The next generation of stars forms from this mixed material (and material produced in stellar collisions), and so on.

The observations of present abundances are based on spectra of interstellar clouds and stellar surfaces. To obtain the primordial abundances from the present abundances the effect of chemical evolution has to be estimated. Since ^2H is so fragile (its binding energy is so low), BBN is the only significant source of ^2H , which is destroyed rather than created in stars. Therefore any interstellar ^2H is primordial. The smaller the fraction of processed material in an interstellar cloud, the higher its ^2H abundance should be. Thus all observed ^2H abundances are lower limits to the

primordial ^2H abundance⁵. Conversely, stellar production increases the ^4He abundance. Thus all ^4He observations are upper limits to the primordial ^4He . Moreover, stellar processing produces heavier elements, such as C, N, and O, which are not produced in BBN. Their abundance varies a lot from place to place, giving a measure of how much chemical evolution has happened in various parts of the universe. Plotting ^4He vs. these heavier elements, we can extrapolate the ^4He abundance to zero chemical evolution to obtain the primordial abundance.

The elements ^3He and ^7Li are both produced and destroyed in stellar processing, making it more difficult estimate their primordial abundance. The observational determinations of the primordial ^3He abundance are currently not at the level of that of ^2H and ^4He . The determination of the primordial abundance of ^7Li from observations remains subject to uncertainty. It used to be thought that it could be determined reliably from stars that are poor in heavier elements, with a plateau in the abundance of ^7Li that is independent of the heavy element fraction and therefore primordial. The resulting value of ^7Li is inconsistent with BBN predictions (as can be seen from figure 4). In recent years, it has been found that there is no plateau, which probably solves the *Lithium problem*. However, like for ^3He , there is still no reliable observational determination of the primordial ^7Li abundance with an accuracy comparable to that for ^2H and ^4He .

There are two clear qualitative signatures of big bang nucleosynthesis in the present universe:

1. All stars and gas clouds observed contain at least 23% ^4He . If all ^4He had been produced in stars, we would see similar variations in the ^4He abundance as we see for the other elements, such for C, N, and O, with some regions containing just a few % or even less ^4He . This universal minimum amount of ^4He signifies primordial abundance produced when matter in the universe was uniform.
2. The existence of significant amounts of ^2H in the universe is a sign of BBN, since there are no known astrophysical sources of large amounts of ^2H .

The observed abundances of the BBN isotopes, ^2H , ^3He , and ^4He indicate the range (mostly determined by the ratio D/H) $\eta = (6.040 \pm 0.118) \times 10^{-10}$ [1]. The agreement between different isotopes and the value determined independently from the CMB provides strong support for this value.

The value $\eta = (6.040 \pm 0.118) \times 10^{-10}$ corresponds to $100\omega_b = 2.205 \pm 0.043$. With $h = 0.7$, we get

$$\Omega_{b0} = 0.04 \dots 0.05 . \quad (5.24)$$

This is much less than the cosmological observational estimates for Ω_{m0} . Therefore they, together with BBN, provide strong evidence that most matter in the universe is non-baryonic; we will discuss dark matter in the next chapter. We can also compare the value of ω_b to the one inferred from the CMB, $100\omega_b = 2.237 \pm 0.015$, a remarkable agreement [4].

⁵This does not apply to sites which have been enriched in ^2H due to separation of ^2H from ^1H . Deuterium binds into molecules more easily than ordinary hydrogen. Since deuterium is heavier than ordinary hydrogen, deuterium and molecules involving deuterium have lower thermal velocities and do not escape from gravity as easily. Thus planets tend to have high deuterium-to-hydrogen ratios.

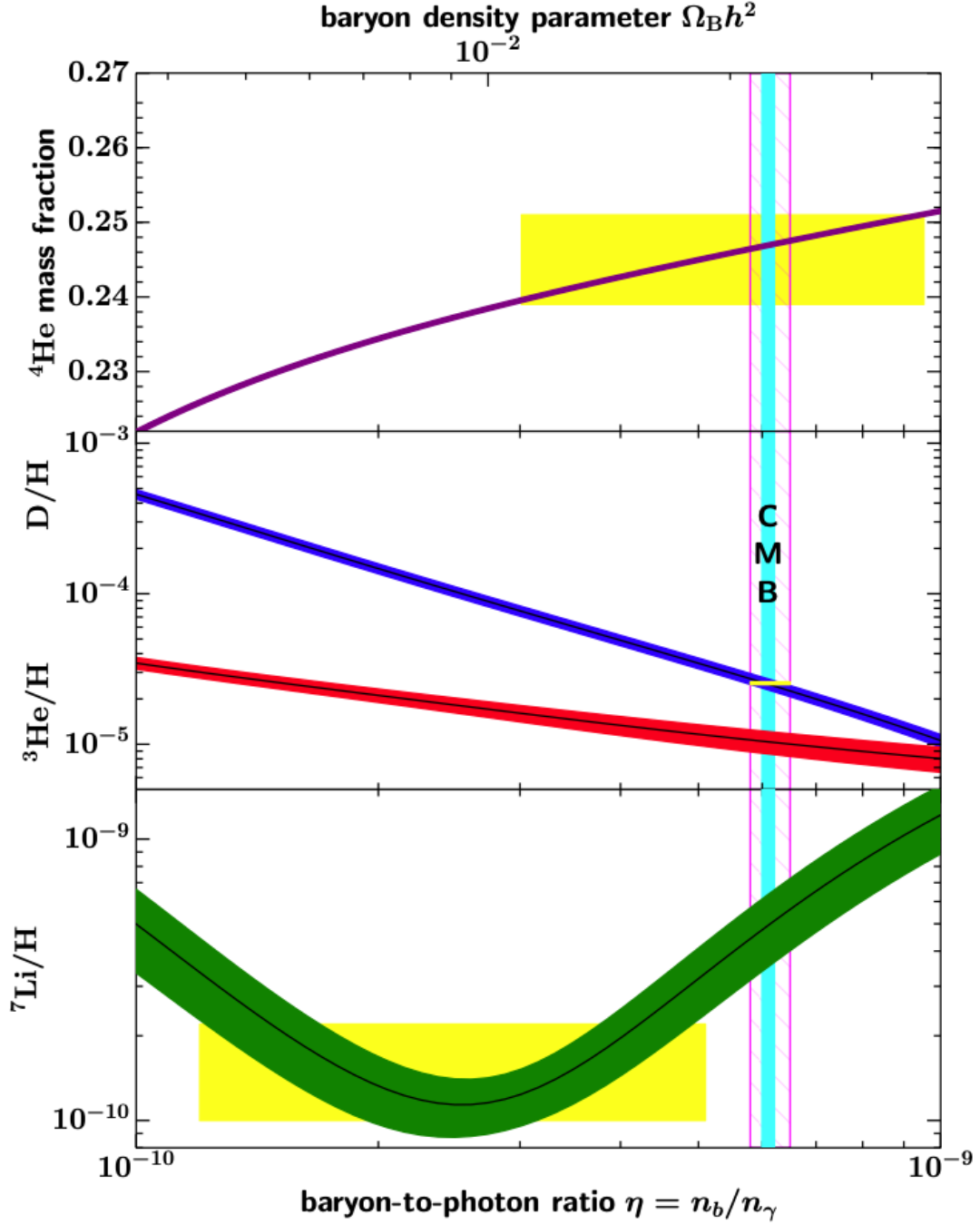


Figure 4: The abundances of ^4He , D , ^3He , and ^7Li and the range of η determined from BBN (yellow boxes) and the CMB (narrow light blue strip) [1]. Both the BBN and the CMB ranges indicate the 95% confidence level. The wider narrow blue strip is determined from the observed D and ^4He abundance.

BBN can be used to probe physics beyond the Standard Model. The expansion rate of the universe depends on the energy density of radiation, encoded in g_* . During BBN, we have $g_* = 5.5 + 1.75N_\nu$, where N_ν is the number of neutrino species with masses so small that they are relativistic during BBN and have weak interactions so that their distribution is coupled to the thermal bath until about $T = 0.8$ MeV. The number of neutrino species can also be left as a free parameter, in which case it parametrises any additional radiation degrees of freedom that may be present. As mentioned in the previous chapter, for the Standard Model we have $N_\nu = 3.043$, because neutrinos are not totally decoupled from the thermal bath when electrons and positrons annihilate, so some of the entropy (and energy density) of electrons and positrons is transferred to the neutrinos, hence the 0.046 correction. If we leave N_ν as a free parameter and fit the observation, we get from light element abundances the range $\eta = (6.088 \pm 0.054) \times 10^{-10}$ and $N_\nu = 2.898 \pm 0.141$ [1]. CMB and large-scale structure data gives a similar constraint $N_\nu = 2.97 \pm 0.1$ [5]. There is no room for an extra neutrino species that would have been in thermal equilibrium. We also know from collider and laboratory experiments that there are only three light neutrinos that interact with the weak interaction. There may be *sterile neutrinos*, which do not feel the weak interaction, and are therefore not in thermal equilibrium at BBN, so they would contribute a fractional (and possibly negligible) number of neutrino species to N_ν . Right-handed partners of the left-handed neutrinos of the Standard Model, if they exist, would be sterile neutrinos and an interesting candidate for dark matter.

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