## COSMOLOGY II

Due on November 18 by 14.00.

1. Running of the spectral index. Assuming slow-roll, calculate  $d\varepsilon/d(\ln k)$ ,  $d\eta/d(\ln k)$ , and then  $\alpha_s$  to leading order in the slow-roll parameters.

## 2. Conservation in the super-Hubble limit.

- a) Starting from eqs. (9.8) and (9.10), derive eqs. (9.18) and (9.19).
- b) Show that if  $w = v^2$ , then  $\delta_k = -2\Phi_k$  = constant is a solution in the long-wavelength limit  $k \ll aH$ . (You may assume that  $a \propto t^n$  with n > 1/4 and  $v^2 = \text{constant} \ge 0$ .)
- c) Is this the only solution? If so, explain why. If not, is it the dominant solution at late times?
- 3. No growth of radiation perturbations. Assuming there is only radiation  $(v^2 = w = \frac{1}{3})$ , derive the evolution of  $\Phi_k$  and  $\delta_k$  in the deep sub-Hubble regime  $(k \gg aH)$ .
- 4. Growth of matter perturbations. Assuming there is only matter  $(v^2 = w = 0)$ , derive the evolution of  $\Phi_k$  and  $\delta_k$  in the deep sub-Hubble regime  $(k \gg aH)$ .