

## ExerciseCosineTwo: Introduction

The **linear** model in **ExerciseCosineOne** is

$$g(t) = M + B \cos t + C \sin t,$$

where  $\bar{\beta} = [M, B, C]$  are the free parameters having errors  $\sigma_{\bar{\beta}} = [\sigma_M, \sigma_B, \sigma_C]$ . The argument units are  $[t] = \text{radians}$ . In that **ExerciseCosineOne**, you are asked to derive the following **analytical equations (i.e. exact solutions)**.

(a) The peak to peak amplitude  $A$  of this model is the difference between the maximum value  $g_{\max}$  of  $g(t)$  and the minimum value  $g_{\min}$  of  $g(t)$ . Solve  $A \pm \sigma_A$  from the given known  $B \pm \sigma_B$  and  $C \pm \sigma_C$  values.

(b) The primary minimum  $t_{\min}$  of this model fulfils  $g(t_{\min}) = g_{\min}$ . Solve  $t_{\min} \pm \sigma_{t_{\min}}$  from the given known  $B \pm \sigma_B$  and  $C \pm \sigma_C$  values.

**Your**  $A$ ,  $\sigma_A$ ,  $t_{\min}$  and  $\sigma_{t_{\min}}$  solutions can contain **only** parameters  $B$ ,  $\sigma_B$ ,  $C$  and  $\sigma_C$ .

## ExerciseCosineTwo: Problem

Use free parameter values  $M = \mathbf{M=1}$ ,  $B = \mathbf{B=1}$ ,  $C = \mathbf{C=1}$ ,  $\sigma_B = \mathbf{eB=0.1}$  and  $\sigma_C = \mathbf{eC=0.1}$ . Assume Gaussian  $B$  and  $C$  distributions, where the standard deviations are  $\sigma_B$  and  $\sigma_C$ .

Edit your **python** program **ExerciseCosineTwo.py**, which solves and prints **numerical**  $A$ ,  $\sigma_A$ ,  $t_{\min}$  and  $\sigma_{t_{\min}}$  estimates.

Send your **ExerciseCosineTwo.py** program to the assistant

**Tip 1.** In your model simulations, use 10000 time point values  $t_i = \mathbf{T}$  between 0 and  $2\pi$ .

**Tip 2.** Your program should give about the same results as those printed below

```
('Results from ', 1000, 'simulated data samples are')
('A=', 2.8311890906257715)
('A error =', 0.19988739465989339)
('tmin=', 3.9286225602115157)
('tmin error=', 0.070263545677305833)
```