

CMB Physics (fall 2007)

P. POLARIZATION

P1. Classical Monochromatic Plane Wave

Stokes parameters, Rotation of coordinates

P2. Classical Quasi-Monochromatic Plane Wave

Coherence tensor, Measurement by a linear polarimeter

P3. Quantum Treatment: One-Photon System

Rotation of coordinate system, Helicity basis,

P4. Quantum Statistical Physics: Density Operator

Pure state, Expectation values, Summary

P5. Statistical One-Photon System

Pure and mixed states

P6. Fock Space

P7. Statistical Many-Photon System

P7.1 Classical N-body and 1-body Phase Space

Identical particles

P7.2 Quantum Many-Particle System and Reduced Density Operator

1-particle operators, Reduced density operator

P7.3 Application to Stokes Parameters

P8. Including Different Momentum States; Observing

Brightness in SI units, Polarization-Sensitive Detector, Collecting area

P9. Photon in Thermal Equilibrium

P10. CMB Perturbations

Perturbations in CMB temperature and occupation number, The polarization tensor

Appendix: Detector Beam

Intensity, Euler angles, Rotating the detector and its beam, 2nd definition of Euler angles,

Circularly symmetric beam, Asymmetric beam and polarization

Appendix: Conversion Factors and Units

CMB and antenna temperature

Y. SPHERICAL HARMONIC EXPANSION OF THE POLARIZATION FIELD

- Y1. Flat-Sky Approximation
- Y2. Geometry of the Sphere
- Y3. Tensor Spherical Harmonics
- Y4. Properties of Tensor Spherical Harmonics

Antinodes, N-S reflection, N and S poles

- Y5. Spin-2 Spherical Harmonics

E and B modes, Properties of spin-2 spherical harmonics

- Y6. Correlation Functions and Angular Power Spectra

y_s^m

F. COLLISIONLESS BOLTZMANN EQUATION

(T only, taught before polarization)

- F1. Phase Space and the Distribution Function
- F2. Energy Tensor in the Local Orthonormal Frame
- F3. Photon Redshift and Free Streaming
- F4. Brightness Equation
- F5. Fourier and Spherical Harmonic Expansion
- F6. Spherical Harmonics (spin-0)

Rotation of ind. system, Product of two spherical harmonics (CG series)

- F7. Generation of CMB Anisotropy by Metric Perturbations
- F7.1 Scalar Perturbations
- F7.2 Vector Perturbations
- F7.3 Tensor Perturbations
- F7.4 Summary
- F8. Free Streaming

C. COLLISIONAL BOLTZMANN EQUATION

- C1. Thomson Scattering
- C2. The Case of Unpolarized Incident Radiation
- C3. Boltzmann Equation
 - 1) Doppler effect, 2) Effect of anisotropy and polarization, The full collision term, Fourier transform
- C4. Wigner D-functions
 - CG series (product of two D-functions)
- C5. Spin-s Harmonics

$s y_s^m$

C6. Rotation at the Collision Term

C7. Multipole Expansion

Loss term, Doppler effect, Gains term, Summary of effect at Thomson scattering, What's left

L. LINE-OF-SIGHT INTEGRATION

L1. Boltzmann Equations

L2. Line-of-Sight Integration

L2.1 Temperature anisotropy

L2.2 Polarization

L3. Radial Functions

L4. Optical Depth and Visibility Function

L5. Delta Function Approximation

L6. Angular Power Spectra

L6.1 Inversion and Rotation

L6.2 Primordial Power Spectra

L6.3 Transfer Functions

L6.4 Angular Power Spectra

L7. The Full Set of Equations

L7.1 Energy Tensor Perturbations and Multipoles

L7.2 Neutrino Multipoles

L7.3 Scalar Perturbations

L7.4 Tensor Perturbations

L7.5 Transfer Functions and Calculation of C_L

L8. Approximate Results for C_L

L9. Photon-Baryon Fluid

L10. CAMB Plots of C_L