

# *From actions to answers*

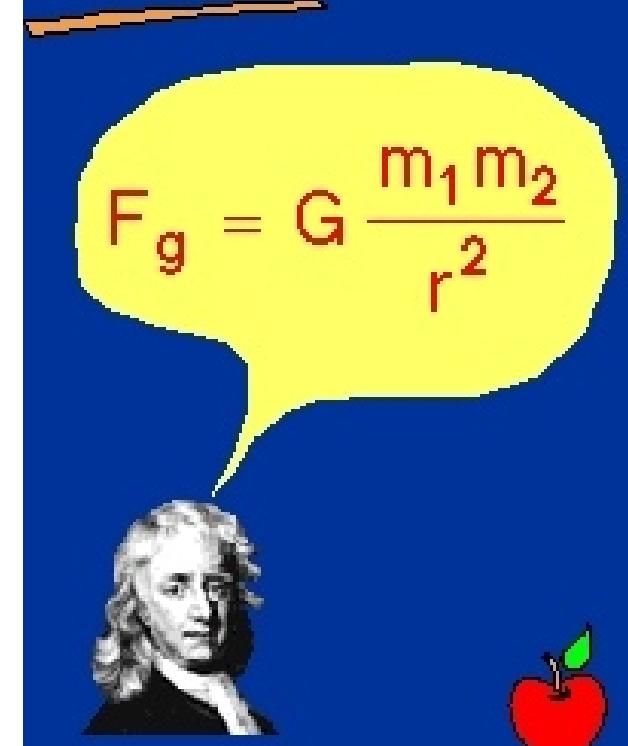
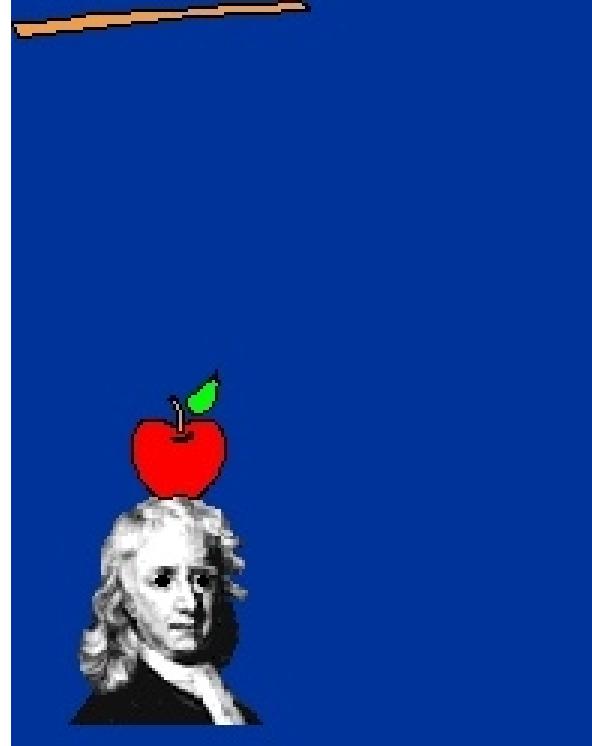
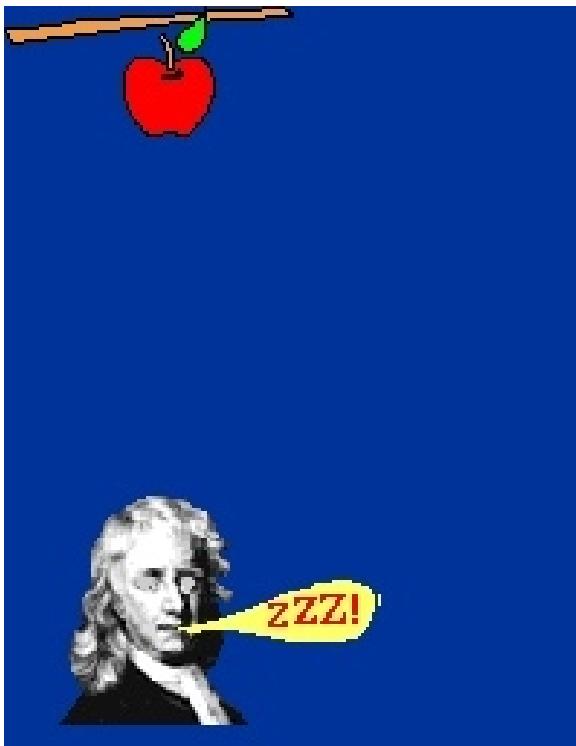
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*University of Helsinki & Oulu  
Departments of Physics*



# *Physics vs. reality*

Explain experiment or observation with ...



*Physics is about numbers!*

**Experiment**

measure

**Theory**

calculate

**Physical quantity, number**

Main duty for theoretical physicists:

***Shut up and calculate!***



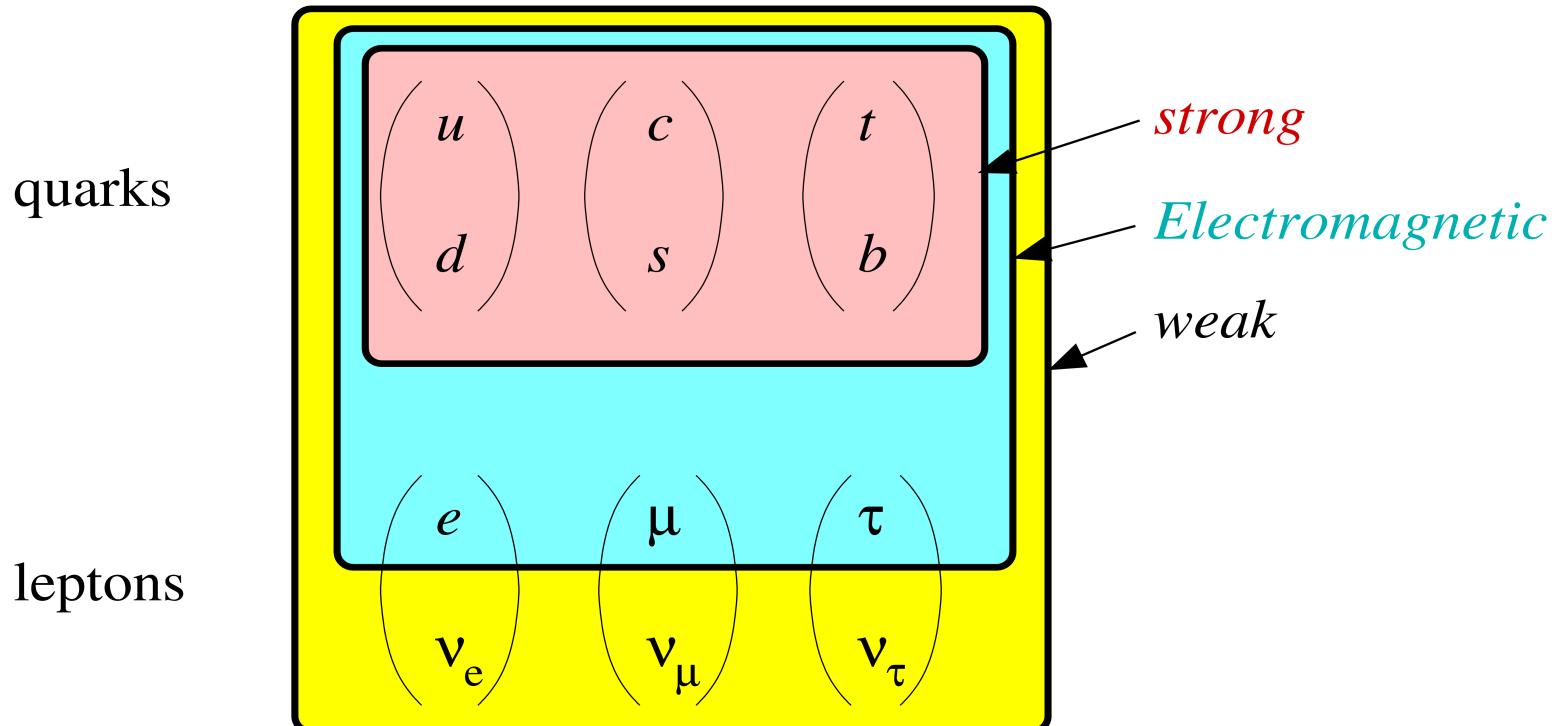
# *The Standard Model (of particle physics)*

Plethora of particles; 3 interactions:

**Electromagnetic (QED)**

**Strong (QCD)**

**Weak**



# The PARTICLE ZOO

## Subatomic Particle Plush Toys

FROM THE STANDARD MODEL OF PHYSICS



**PHOTON**  
The massless wavicle we know and love.



**NEUTRINO**  
These teeny-tiny l'il "shy" guys are traveling through you right now.



**PROTON**  
We would not be here without her positivity.



**WEAK GAUGE BOSON**  
As the carrier particle of the weak nuclear force, he's down-right obese.



**GLUON**  
The "glue" of the strong nuclear force.



**ELECTRON**  
A negatively charged diminutive, busy l'il guy. And popular, too!



**NEUTRON**  
He insists on remaining neutral.



**HIGGS BOSON**  
A bit of a snob because he's sometimes referred to as "the God particle."



**DARK MATTER**  
The mysterious missing mass



**UP QUARK**  
A tiny little point inside the proton and neutron, she is friends forever with the Down Quark.



**MUON**  
A "heavy electron" who lives fast and dies young.



**MESONS**  
A slew of family cousins with names like pion, kaon, rho, and eta.



**GRAVITON**  
Still unobserved, yet theoretically *everywhere*.



**DOWN QUARK**  
A tiny little point inside the proton and neutron, he is friends forever with the Up Quark.



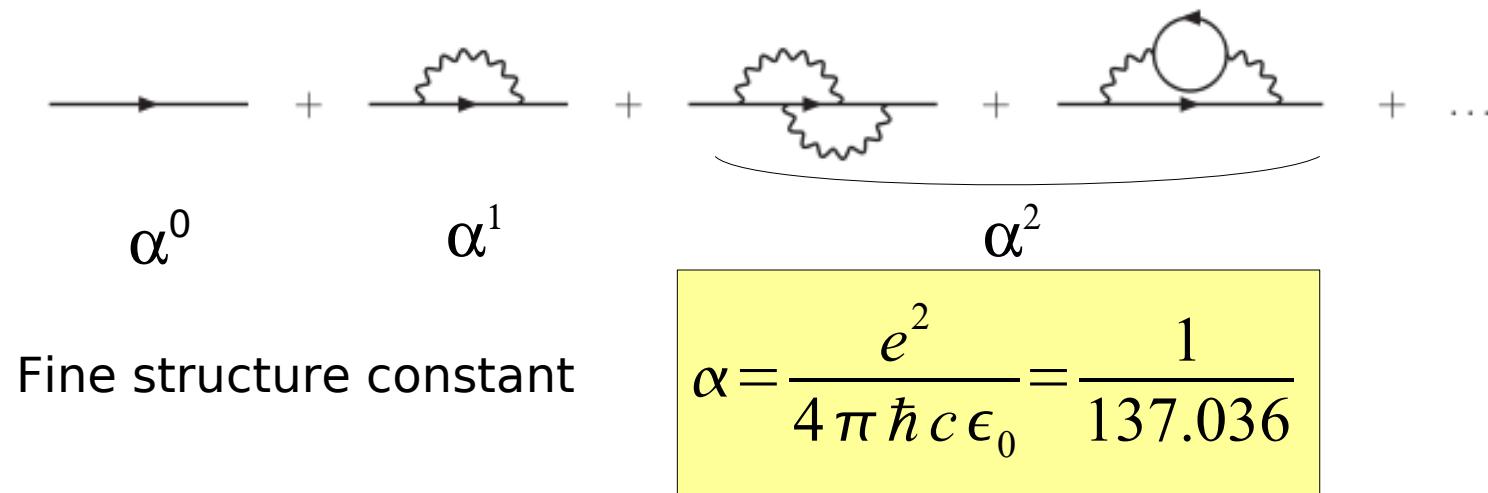
**TAU**  
A "heavy muon" who could stand to lose a little weight.



**ANTIPARTICLES**  
Due to explode on the scene sometime soon.  
**TACHYON**  
Can this particle really travel faster than light?

# *How to compute stuff? 1. Perturbation theory*

- (Semi)analytic, diagrammatic expansion
- Taylor expansion in “coupling constant”
- Works very well in QED:



- Expansion parameter small – rapid convergence!
- Theory/experiment works to precision of  $\sim 10^{-10}$  (best theory ever!)
- Nevertheless, it does not really converge... only asymptotic

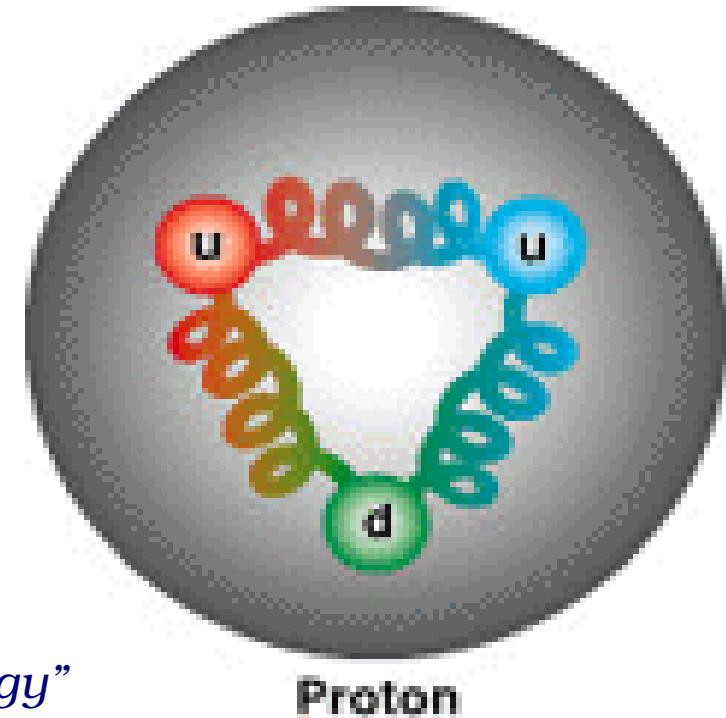


# *How about strong interactions, QCD:*

- Electrons, photons -> **quarks, gluons**
- Quarks & gluons: building blocks of **hadrons** (protons, pions...)
- **Baryon** (proton, neutron,...): 3 quarks
- **Meson** (pion,...) quark-antiquark

What has been observed:

- *There are no free quarks; quarks are always bound within hadrons (confinement)*
- *Mass of proton  $\sim 938 \text{ MeV}$*   
*Mass of  $u,u,d$  -quarks  $\sim 10 \text{ MeV}$*   
*Gluons massless*
- > *99% of proton mass is “binding energy” due to QCD (hence, 99% of the mass of matter)*



***Why? Perturbation theory cannot answer***



# *QCD “running coupling”*

The QCD expansion parameter

$$\alpha_s = \frac{g_s^2}{4\pi}$$

depends on energy of the process:

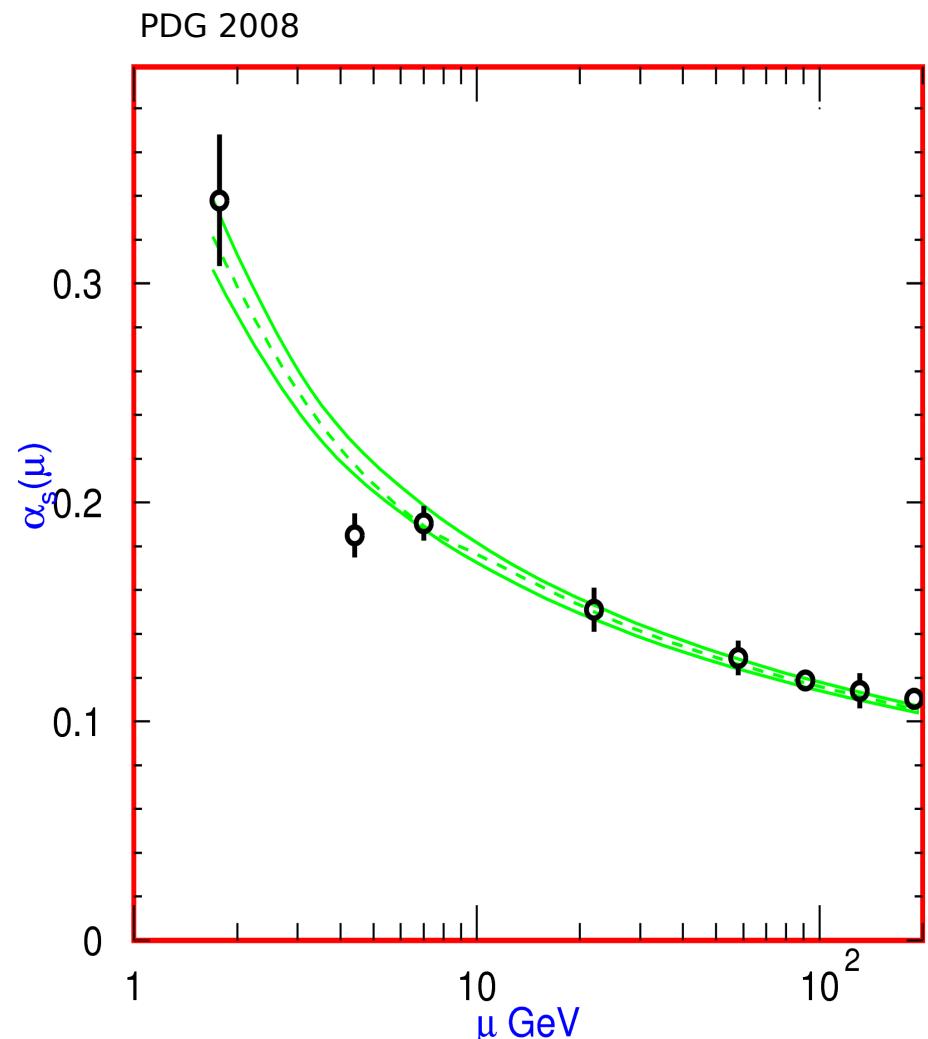
- At large energy  $\mu$   $\alpha_s$  is small  
at LHC,  $\alpha_s \sim 0.12$

-> perturbation theory  $\sim$  OK

- As  $\mu < 1$  GeV (proton mass),  
 $\alpha_s$  diverges (apparently)

**“Strong coupling”, **perturbation theory does not work.****

(Gross, Politzer, Wilczek 1974, Nobel 2004)



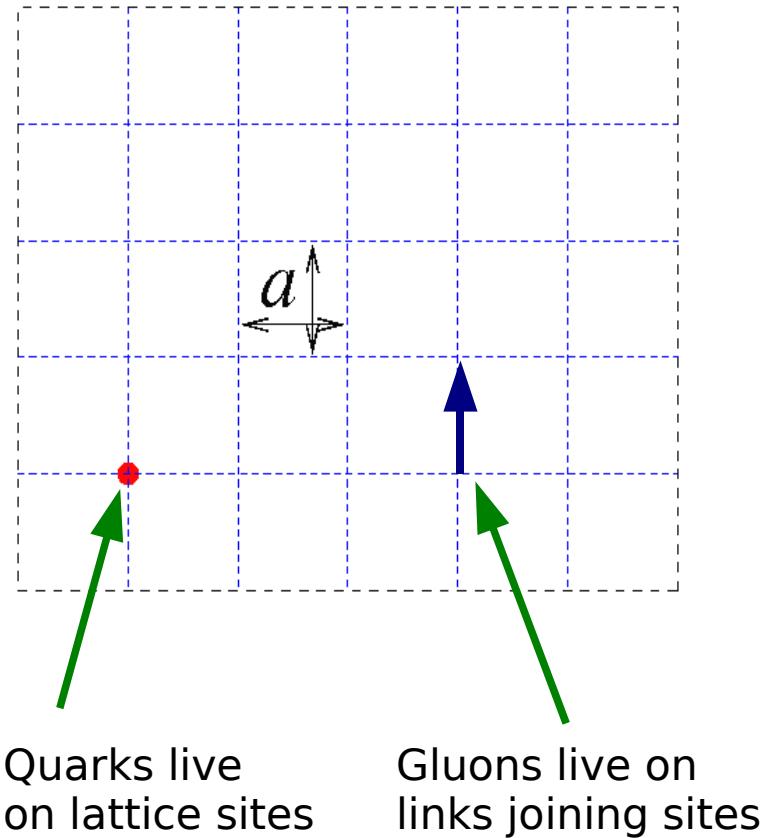
# *QCD on the lattice:*

QCD defined by Feynman path integral

$$Z = \int dA d\psi e^{iS(A, \psi)}$$

Mid-70's Ken Wilson showed how to put quantum field theories (including QCD) on a discrete lattice

- path integral becomes well-defined and finite, suitable for numerical evaluation
- Computer simulations start at end of 70's
- Lattice provides the best *definition* of the theory!

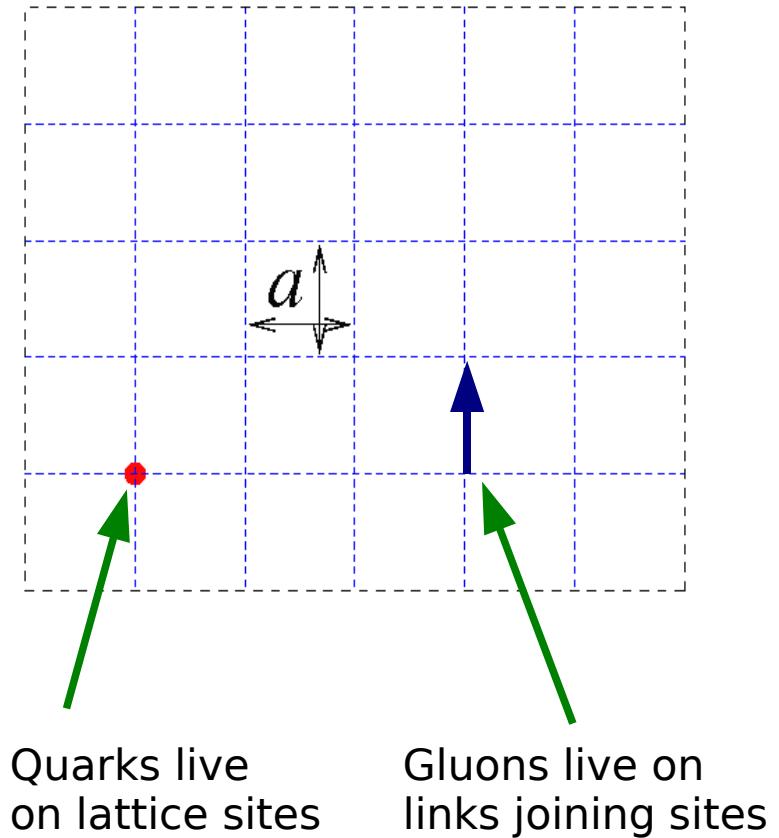


# *Physics in femto-universe:*

Features:

- 4-dim. discrete spacetime lattice
- Lattice spacing  $a$ ; need continuum limit  $a \rightarrow 0$
- Calculate at several different  $a$ , extrapolate  $a \rightarrow 0$   
⇒ full quantum theory, no approximations

- Full QCD simulations very expensive! Only recently accuracy comparable to experiments has been reached.
- Active field, with many subfields:  
~500 participants at the annual “Lattice” conferences



# Why lattice QCD is expensive?

- 4-dimensions
- quantum
- fermions (quarks)

Fermions can be integrated out, but that makes the action *non-local*: *fermion determinant*

$$Z = \int dU d\psi e^{-S_G(U) - \bar{\psi} M(U) \psi} = \int dU \det[M(U)] e^{-S_G(U)}$$

Quenched simulation: just ignore the fermion determinant (not used any more)

Currently largest volumes in use:  $60^4$  -  $100^4$



# *Large-scale computing*

Lattice simulations are large-scale supercomputing projects.  
To get most bang for the buck, some groups design their own  
computers, down to the chip level

**QCDOC, Brookhaven**



# *It works!*

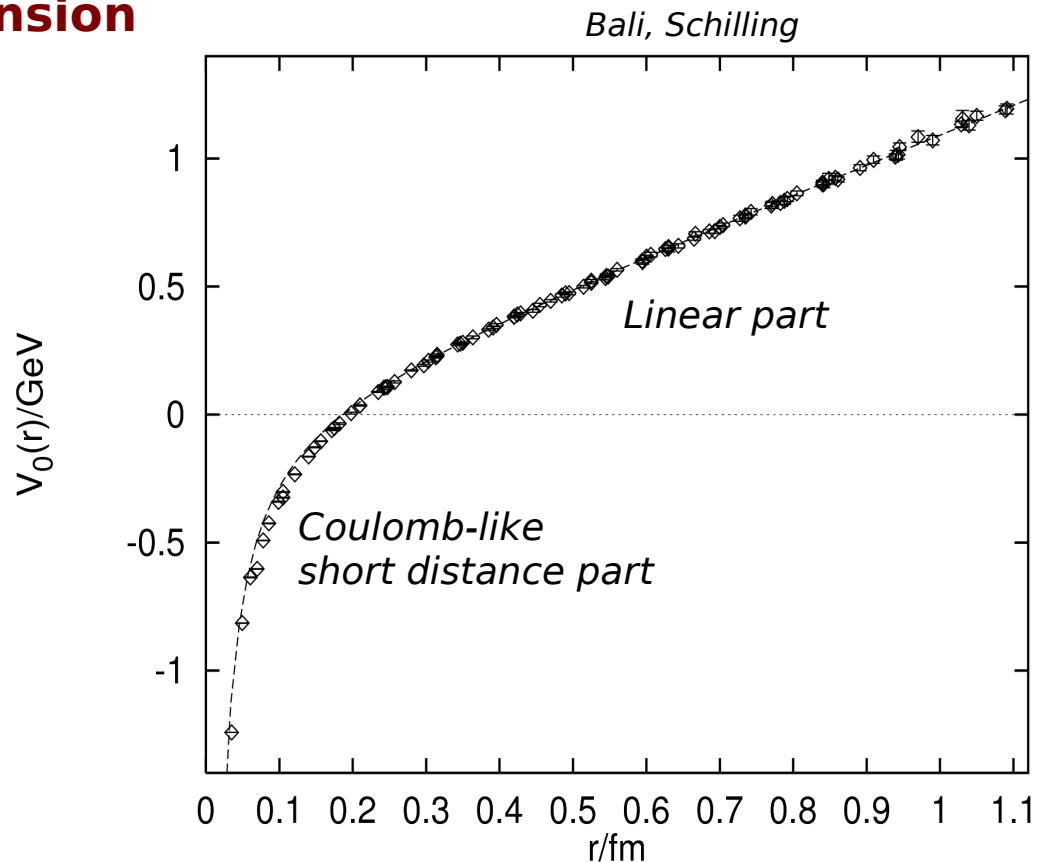
Measure quark-antiquark potential in a meson:

at large distances: linear increase

⇒ constant force, **string tension**

⇒ it takes infinite energy to  
move quarks infinite  
distance from each  
other

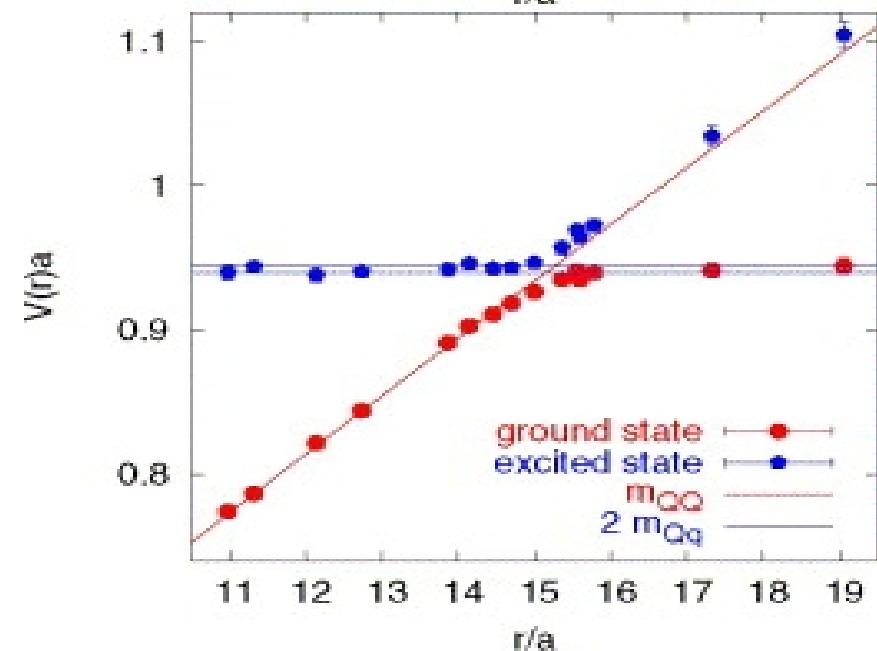
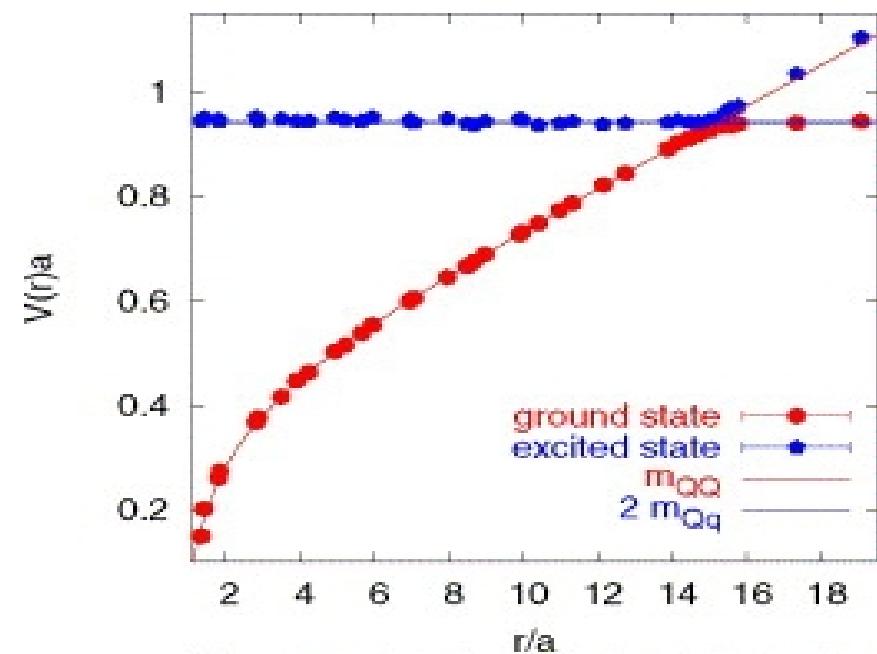
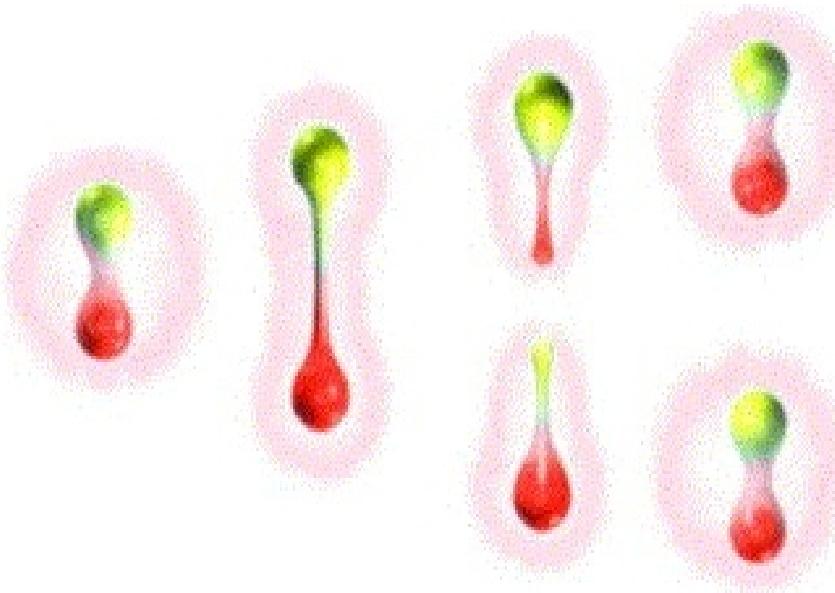
⇒ **quark confinement**



# *String breaking*

In reality, the string breaks forming a new pair of mesons.

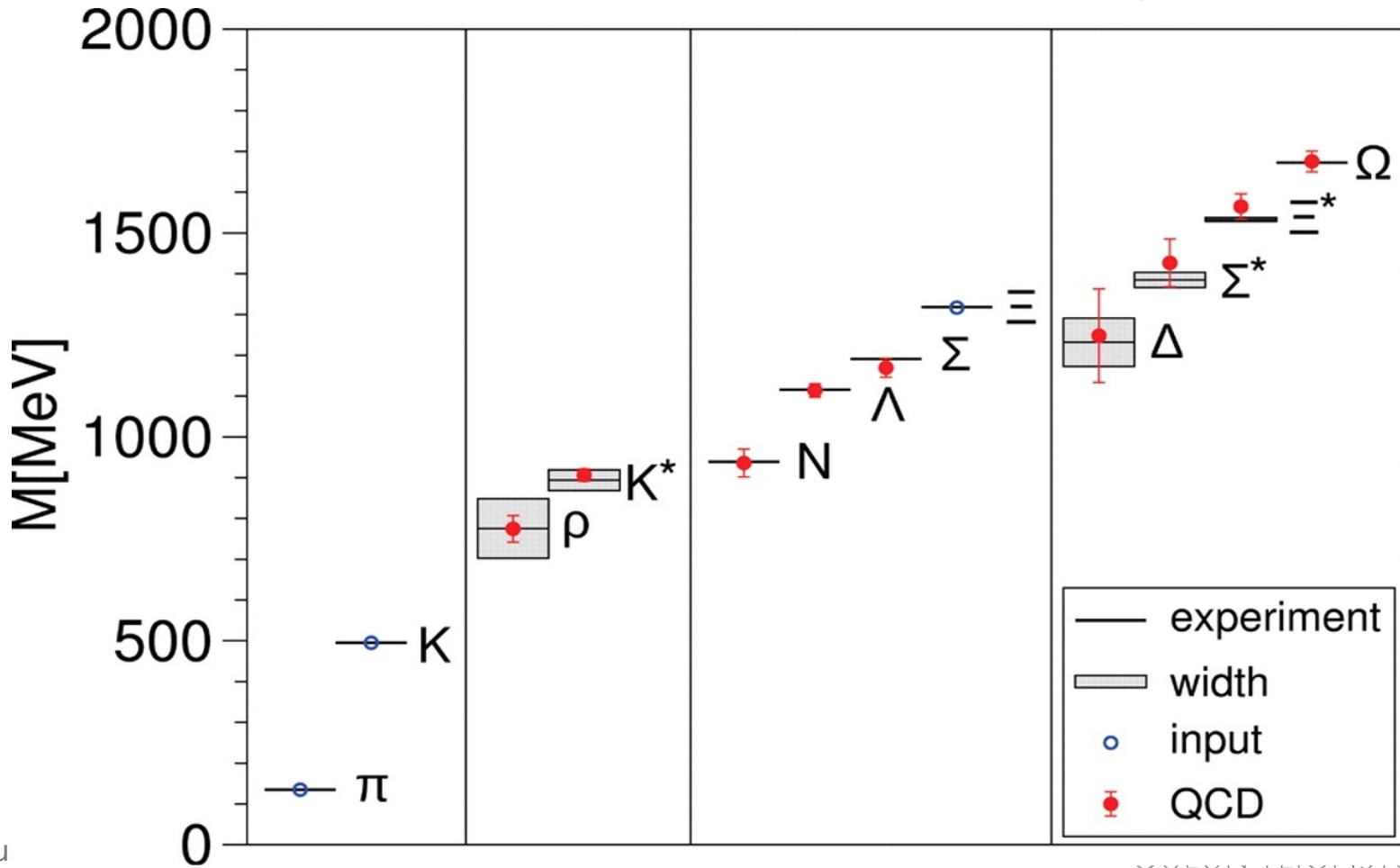
Recently observed in simulations (Attig et al, 2005)



# Hadron masses?

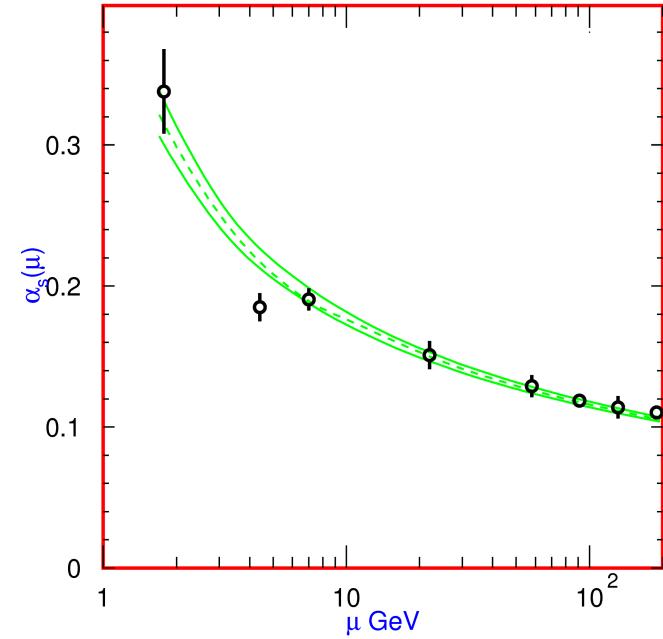
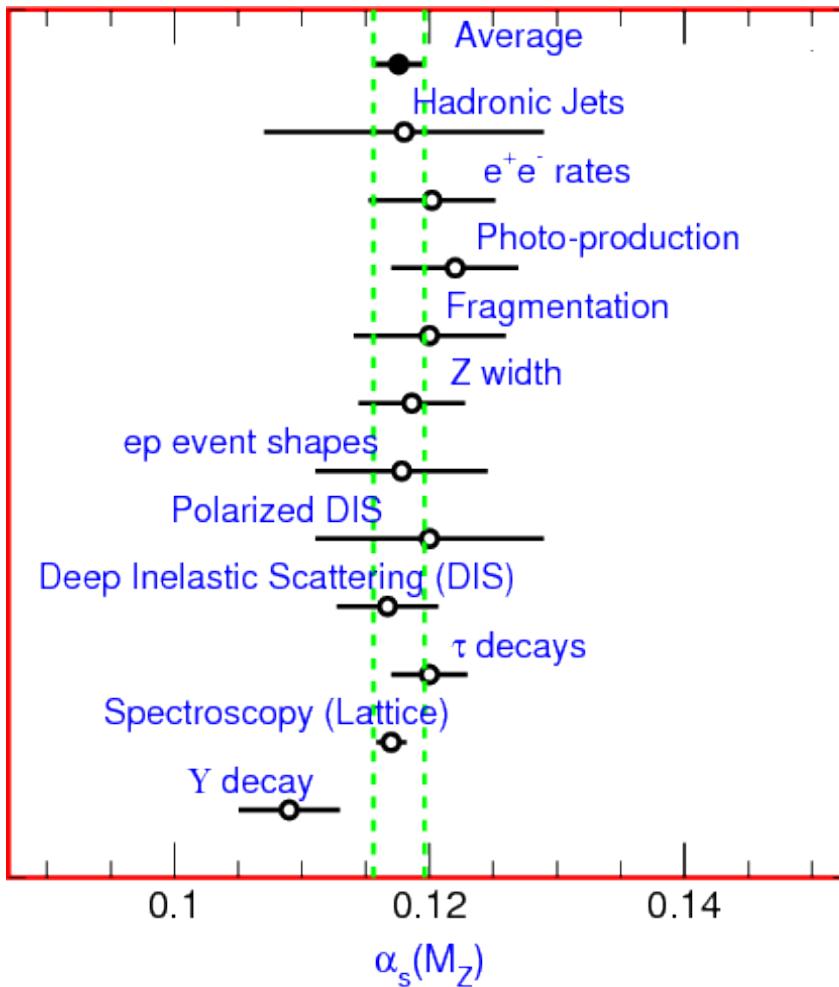
Works very well!

BMW collaboration, Science 2008



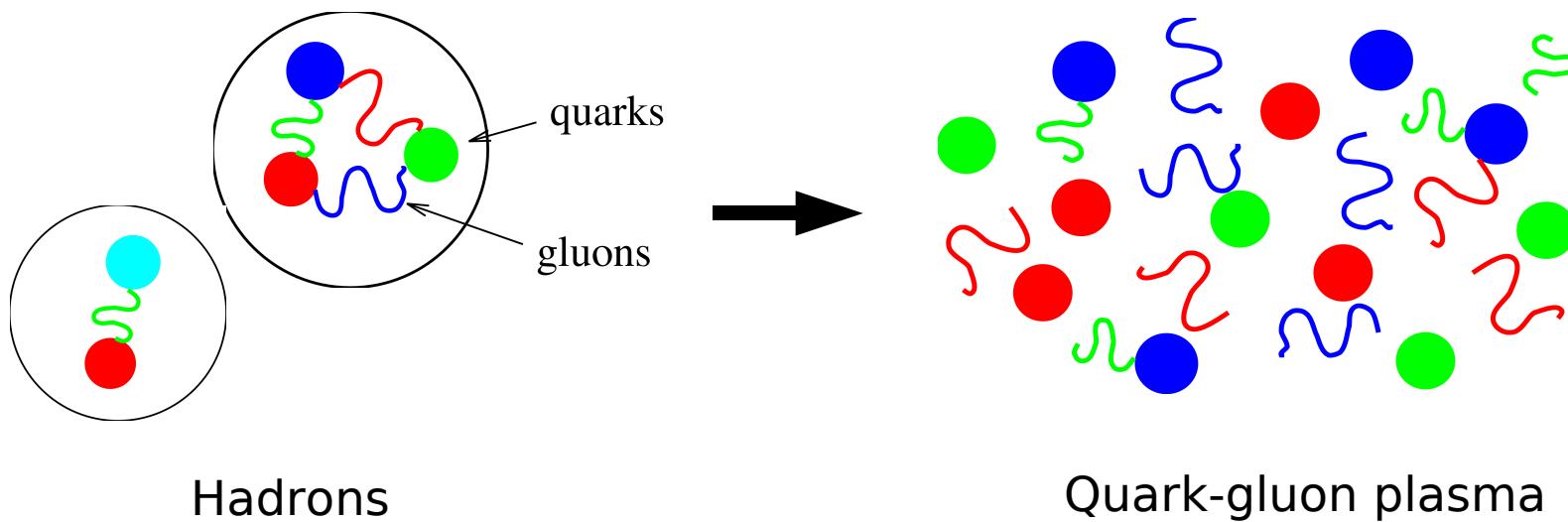
# *Results are competitive with experiments*

$\alpha_s$  at  $M_Z$



## *At high $T$ : quark-gluon plasma*

At high temperature or density, hadrons (protons, neutrons etc.) “melt” and form **quark-gluon plasma**: dense gas of quarks and gluons

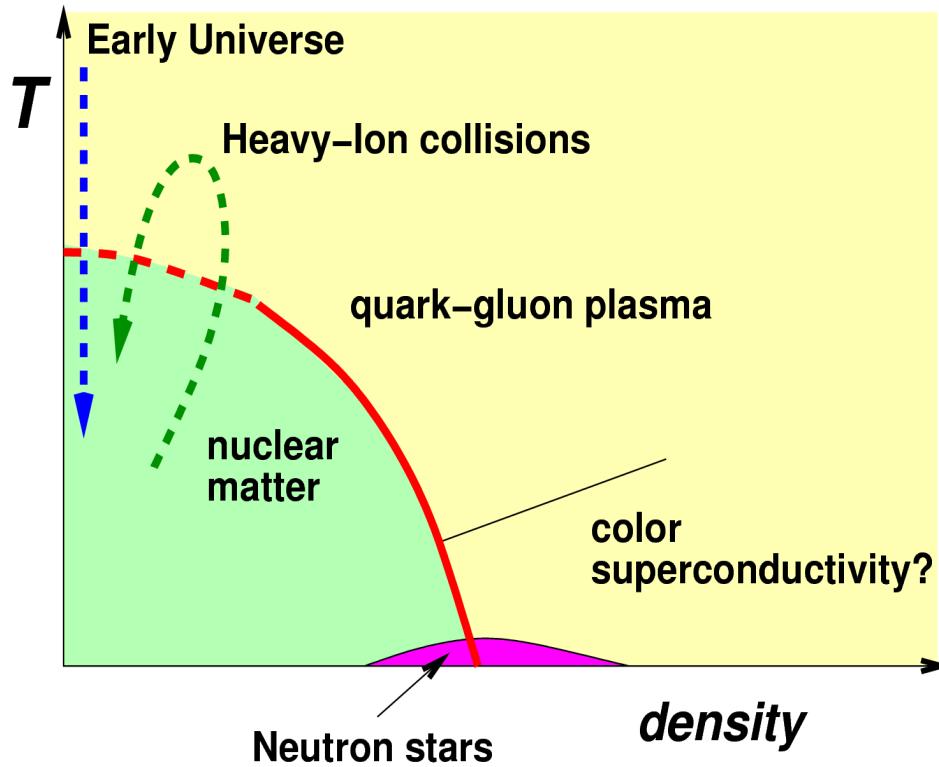


Lattice simulations; experimentally verified (RHIC, Brookhaven)

Transition temperature  $T_c \sim 170$  MeV



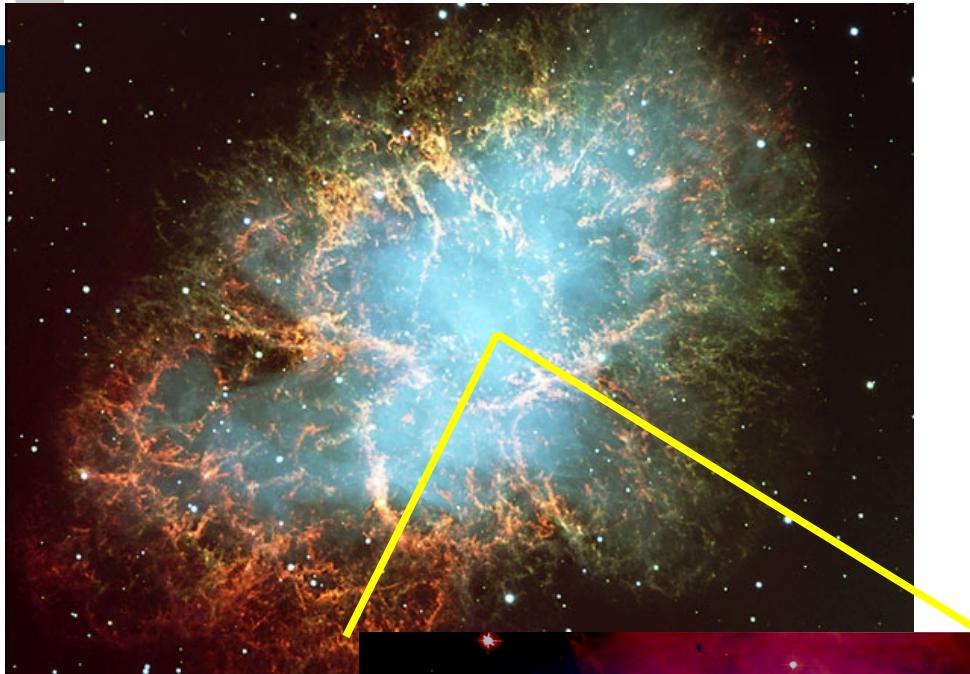
# *QCD phase diagram*



- Quark-gluon plasma (should be) found at high temperature and density
- To study the transition lattice simulations are needed
- Nature of the transition? 1<sup>st</sup> order/continuous?
- Location of the “triple point”?
- Only the low-density region is currently under numerical control: “sign problem”!



# Neutron Stars

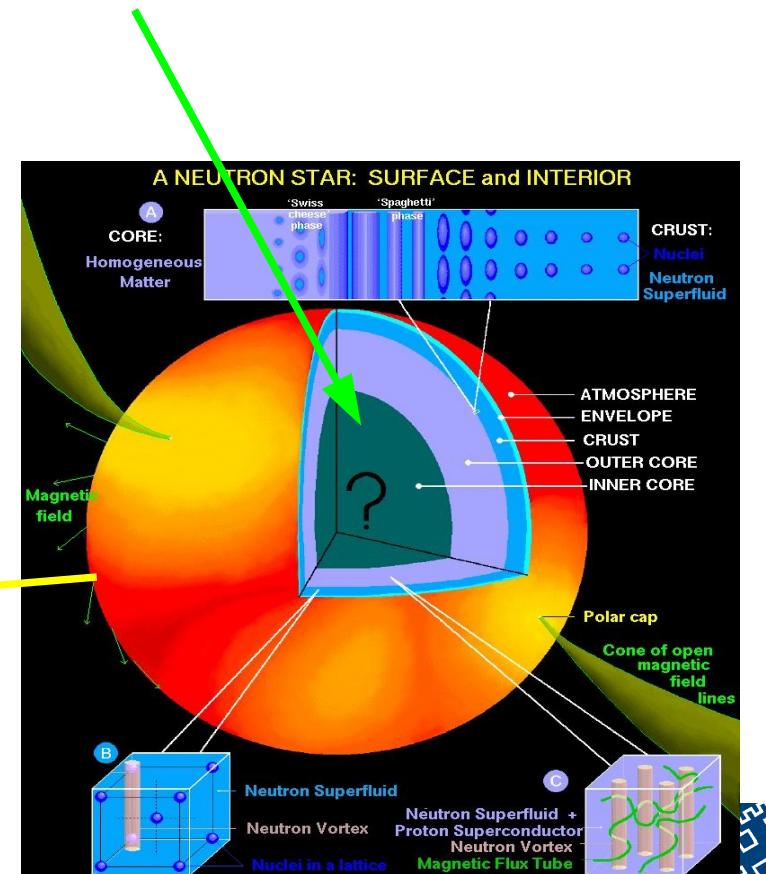


Crab nebula

Kari Rummukainen

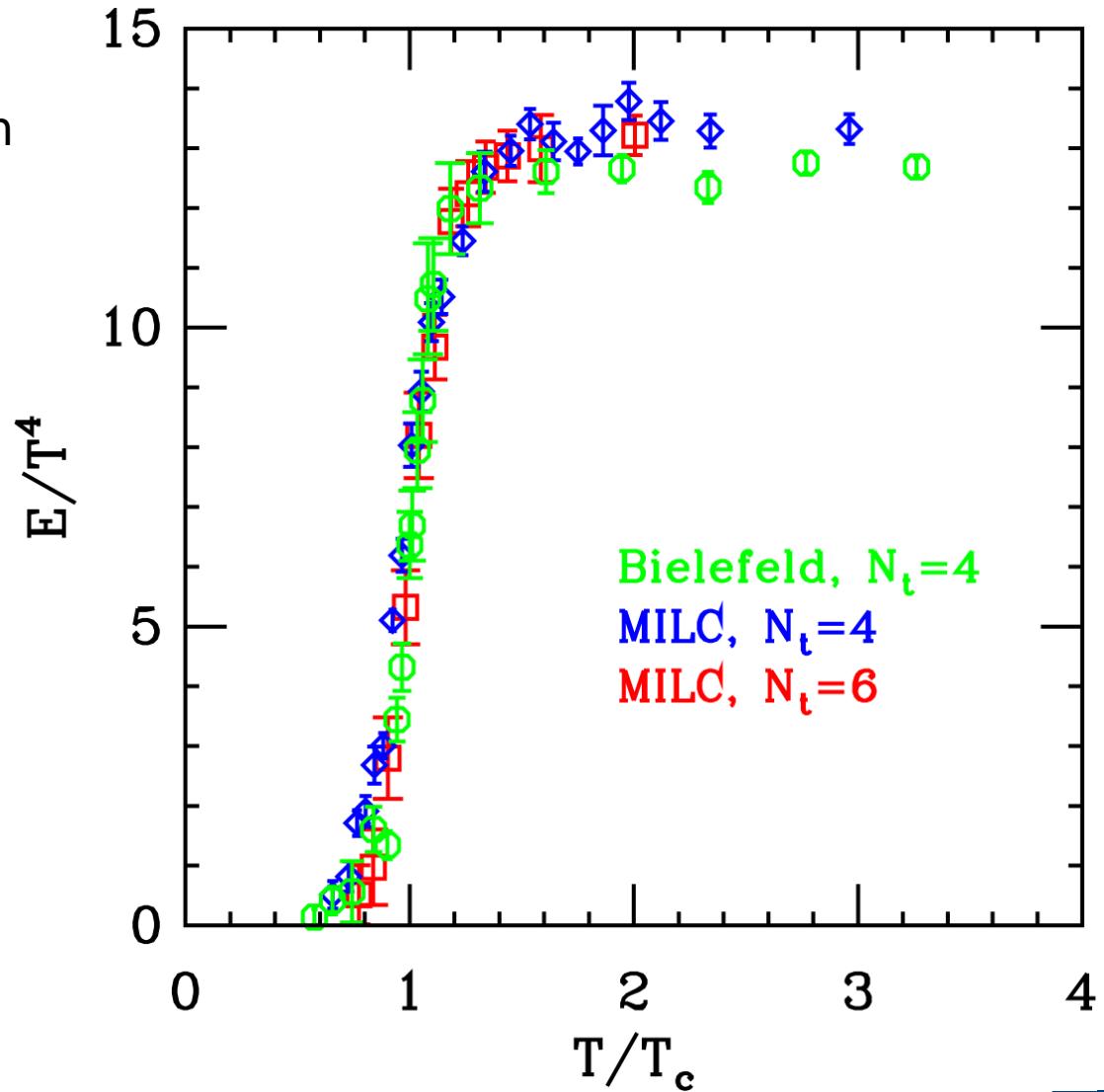
Quark matter core  
inside neutron stars?

Equation of state determines  
stability & maximum size



# *Transition to quark-gluon plasma*

- Phase transition clearly observed in simulations; e.g. energy density:



# *Is QCD perturbative at extremely high T?*

High T  $\rightarrow$  small  $\alpha_s$   
pert. theory  
should work?

Can be studied  
using *effective*  
*theory* simulations

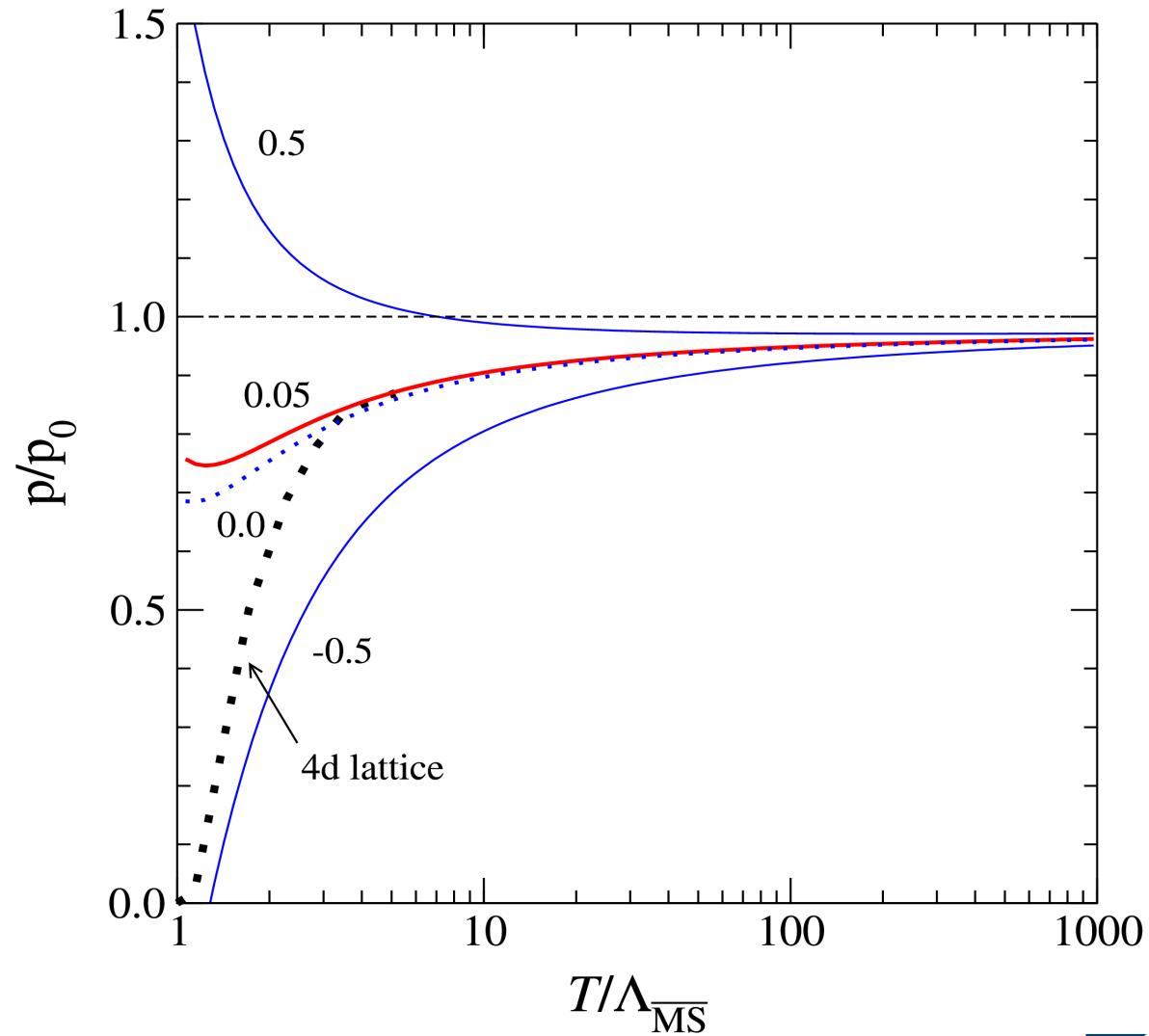
[Hietanen, Kajantie, Laine,  
Rummukainen,  
Schroeder]

P.T. works well  
only at extremely  
high

$T > 100\text{-}1000 T_c$

*Figure: pressure,  
normalized to ideal  
gas*

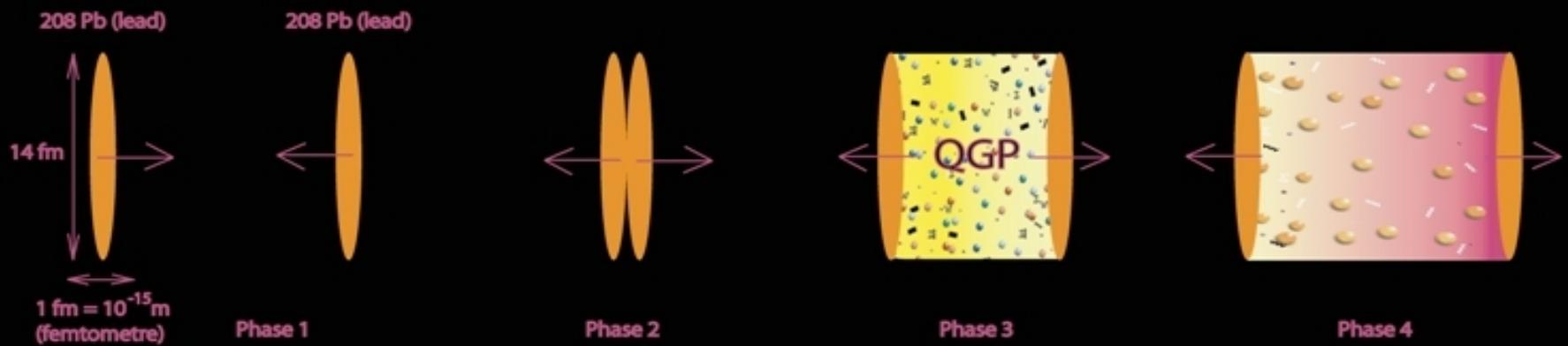
Kari Rummukainen



# *Heavy Ion collision experiments*

Collide two heavy nuclei together at high energy: “little bang”

## PRODUCTION OF QGP



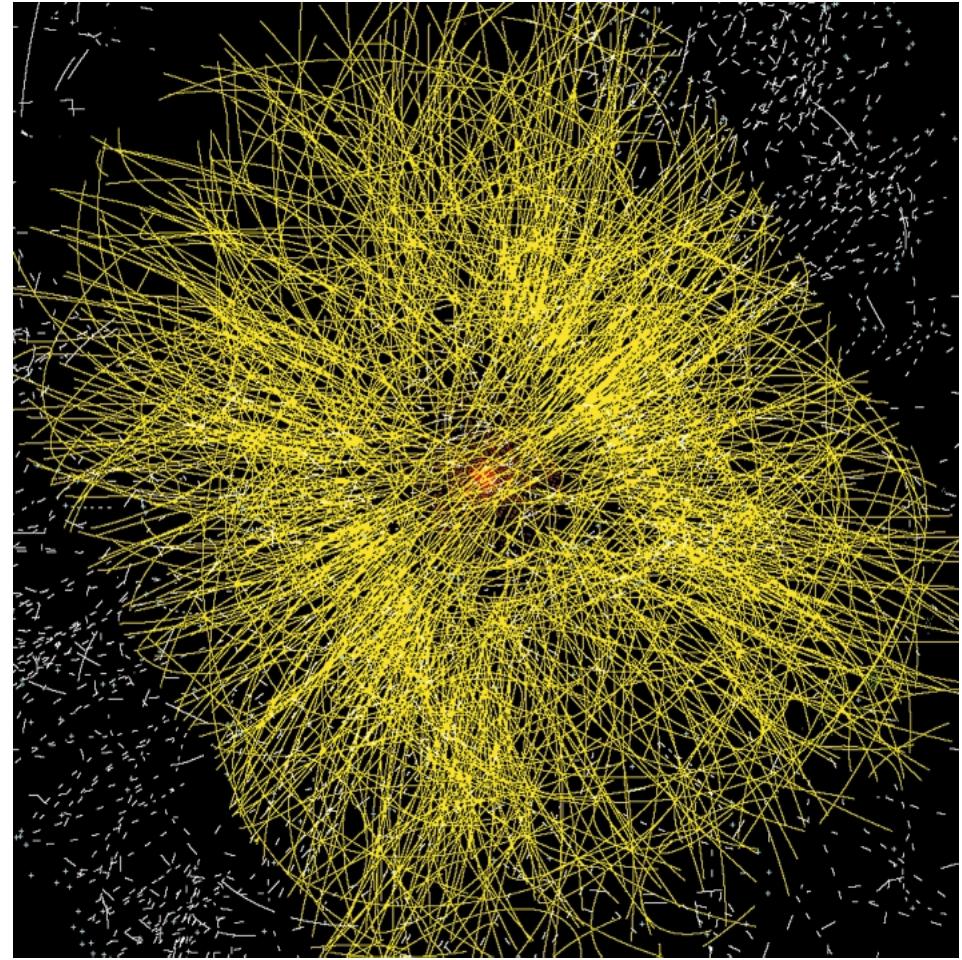
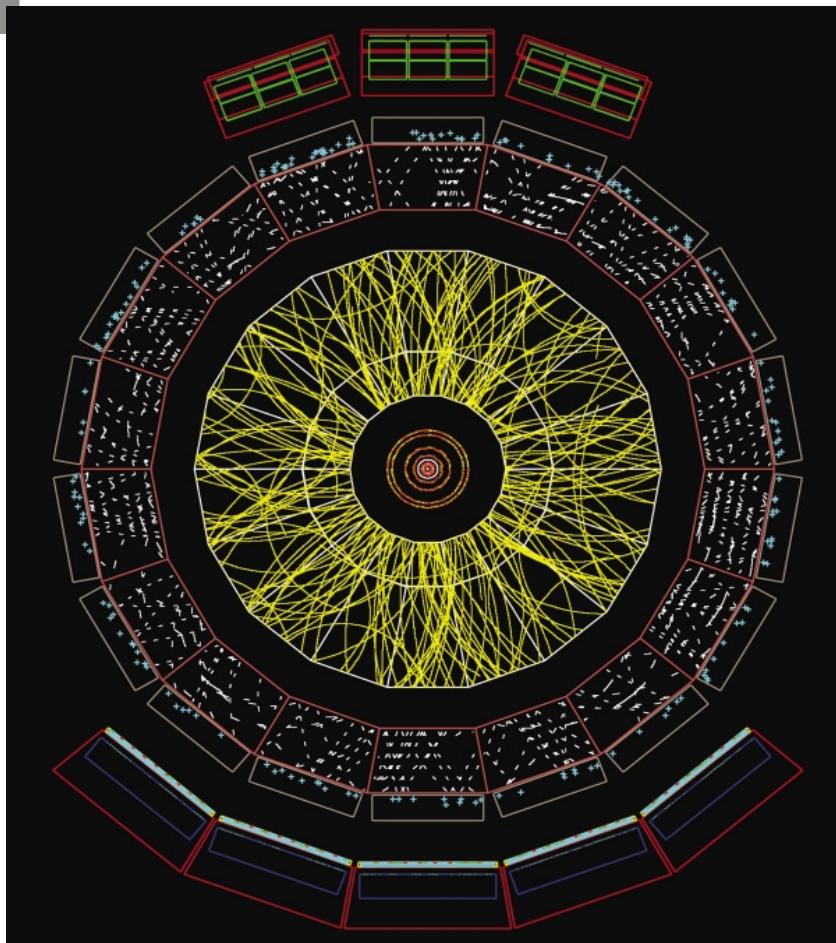
RHIC, Brookhaven; LHC (Alice experiment), CERN; GSI (planned)  
Transient and complicated system!

**Time dependent, off-equilibrium** system: simulations require  
special methods (non-standard lattice simulations)

- Thermalisation? Equation of state? Particle production?



# Alice, Pb-Pb -collision (simulated)



# *QCD plasma instability*

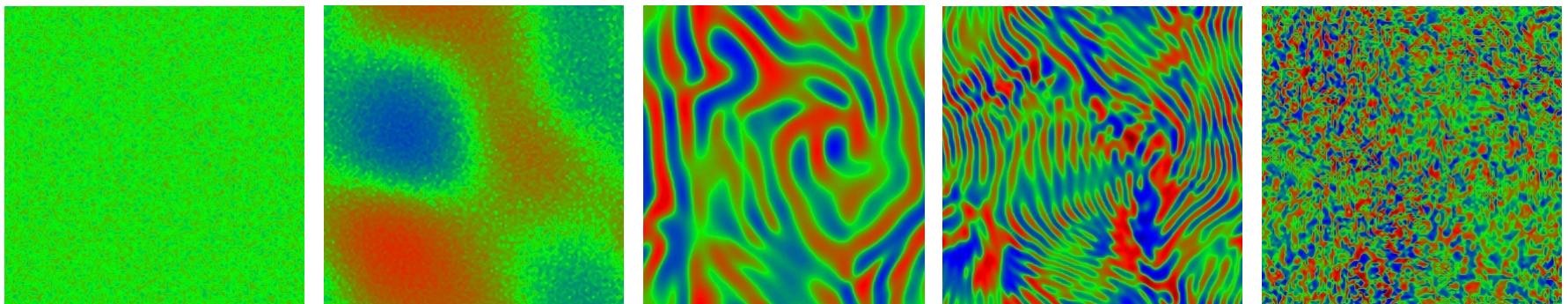
The initial state of Heavy-Ion collision is far from thermal.

Observation (RHIC, 2004-6): plasma is “thermalised” very rapidly, much faster than most estimates suggest. Why?

Non-equilibrium real-time process: requires special methods; HTL effective theory

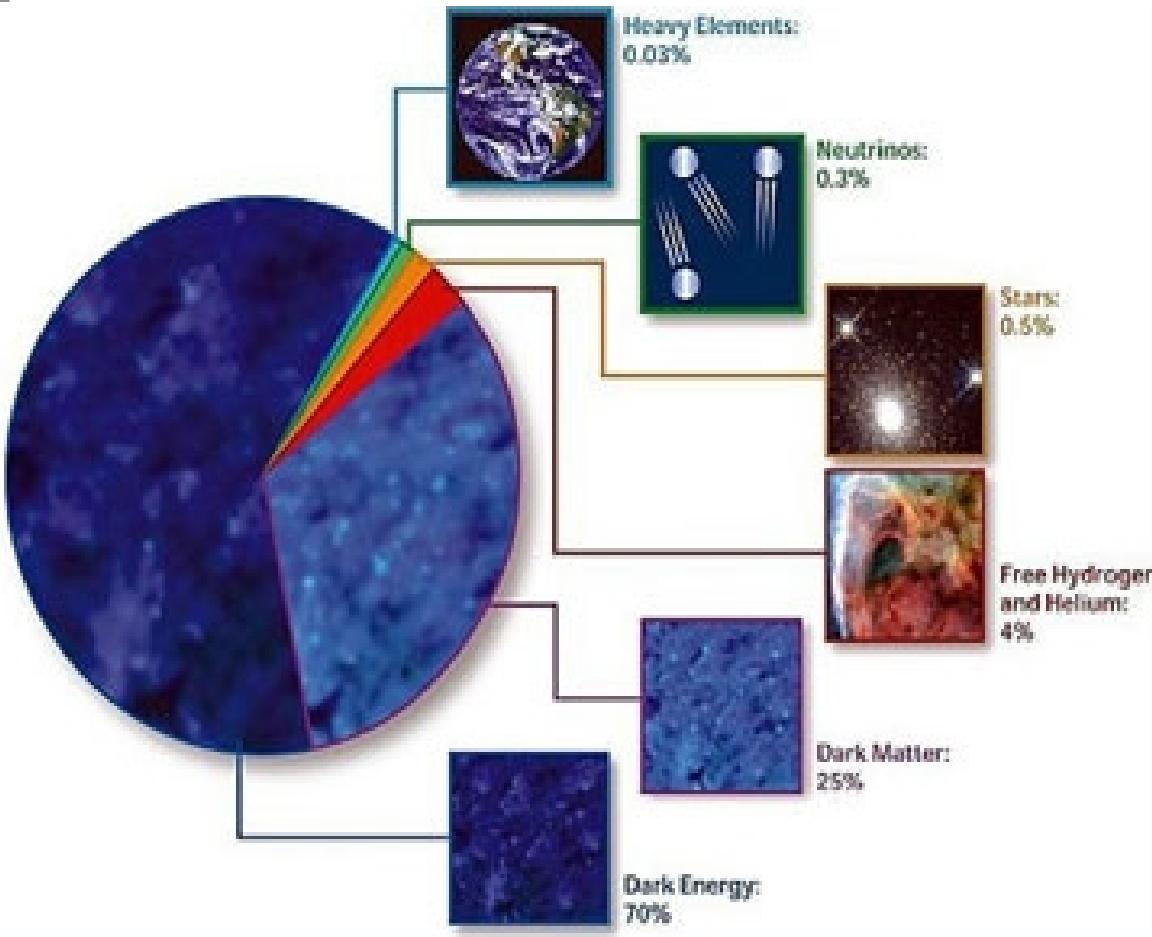
Results: with suitable initial conditions, there is (Weibel) **plasma instability** -> exponential growth in some gluon modes -> rapid thermalisation

[Bödeker, Rummukainen JHEP 0707:022 (2007)]



# *Beyond QCD: Electroweak theory at high T*

Universe contains matter (baryons), not antimatter! **Why?**



Normal stuff: 4-5%  
(known elementary particles)

“Dark”, exotic (unknown) matter 24%

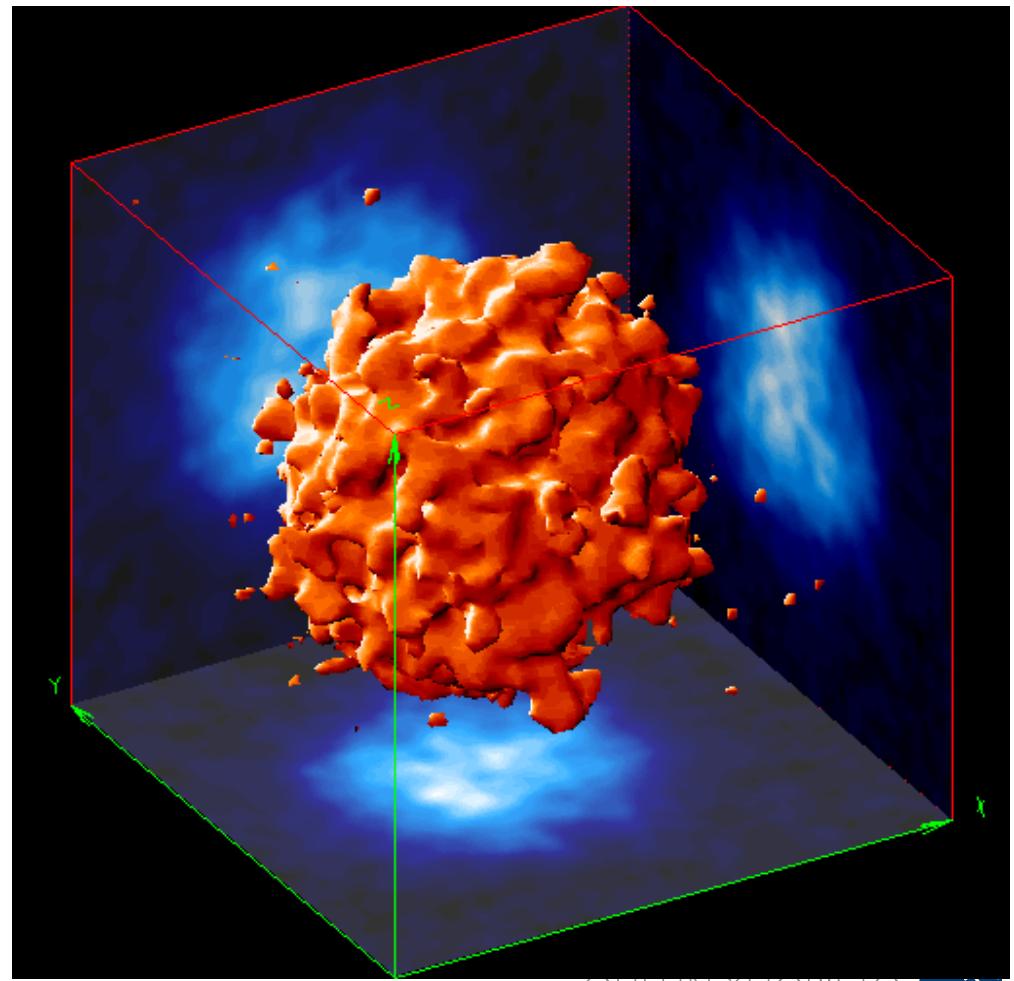
Missing 71%: vacuum energy, “dark energy”.



# Electroweak baryogenesis

- Electroweak phase transition happened in  $\sim 10^{-10}$  s old Universe
- Last possible moment to generate matter-antimatter asymmetry: **baryogenesis**
- If 1<sup>st</sup> order phase transition, it proceeds through *bubble nucleation*
- Matter could be generated on the surface of the growing bubbles
- Does it work? → Lattice simulations

Moore,  
Rummukainen,  
Tranberg



# Electroweak baryogenesis

- Simulations showed that the transition is of 1<sup>st</sup> order only if Higgs mass

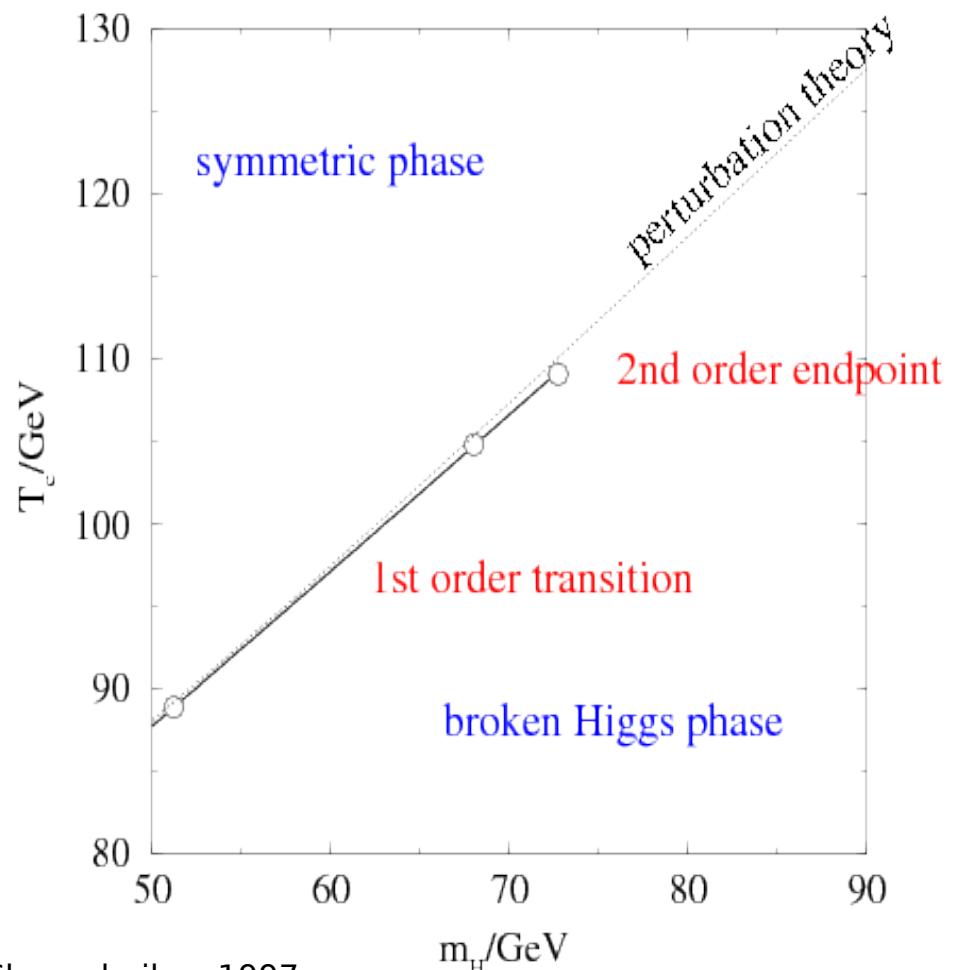
$$m_H < 72 \text{ GeV}$$

- Present experimental limit

$$m_H > 115 \text{ GeV}$$

⇒ EW baryogenesis not possible in the Standard Model

⇒ “*New physics*” required for successful baryogenesis  
(extended electroweak sector, supersymmetry, leptogenesis ... )



Kajantie,Laine,Rummukainen,Shaposhnikov 1997



## *Finally:*

- From the very beginning, lattice simulations have been an important *qualitative* tool for studying QCD
- Now also quantitative precision competes with experiments!
- In addition to bread-and-butter QCD calculations, lattice methods can be applied to a wide range of novel problems
- In Finland, we have studied:
  - Electroweak theory
  - Supersymmetry
  - Non-equilibrium physics
  - Extra dimensions
  - Technicolor (with Jyväskylä)
- *Growing research program; lots of interesting problems to be studied!*

